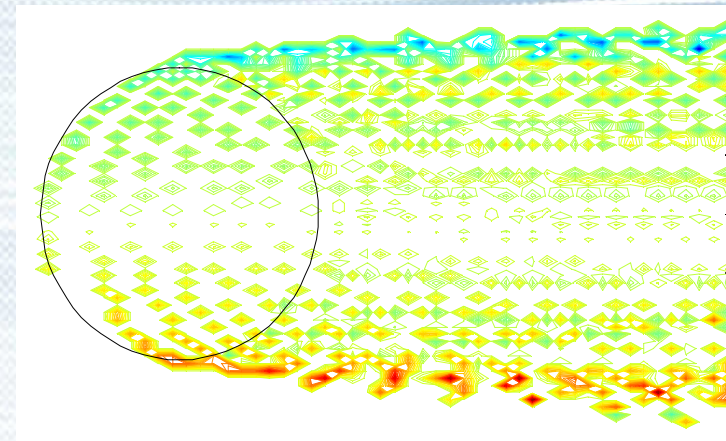
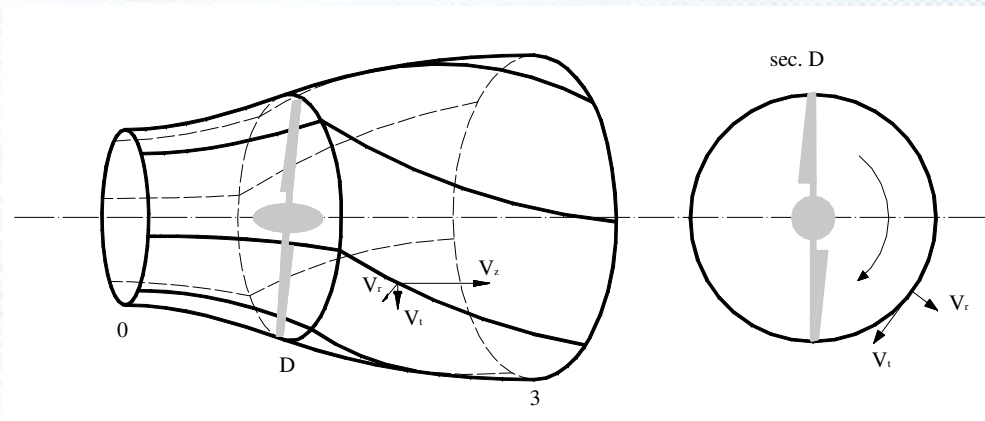




UNIVERSITÀ DEGLI STUDI DI UDINE  
Dottorato in Tecnologie Chimiche ed Energetiche

# FLUID DYNAMIC MODELLING OF WIND TURBINES



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Dottorando:  
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Udine 21 Maggio 2010



# Summary

Introduction

PART I : HAWT analysis

HAWT Fluid dynamics

A turbomachinery approach

Inverse design



# Summary

PART II : VAWT analysis

VAWT fluid dynamics

VAWT experimental analysis

VAWT free vortex wake

Results and conclusions

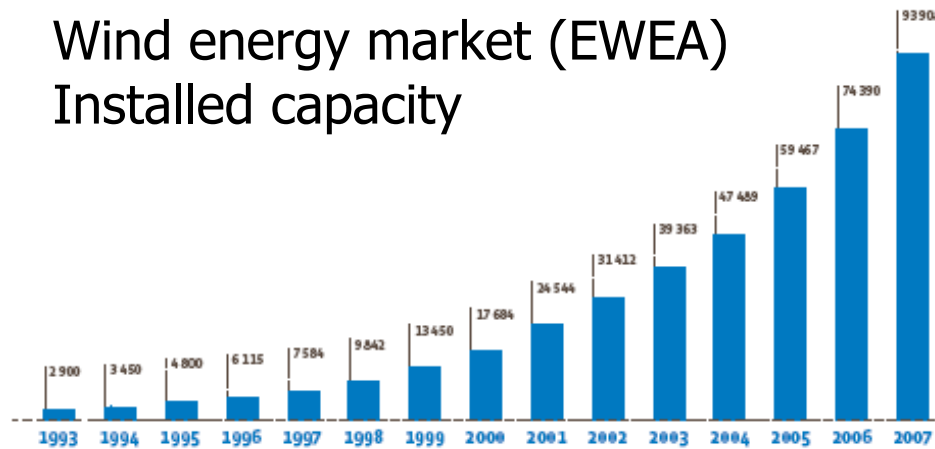


# Introduction

Potenza eolica totale installata nel Mondo dal 1993 (in MW)\*.

\* Stime. Fonte: EurObserv'ER 2009.

Wind energy market (EWEA)  
Installed capacity



Offshore WE market (EWEA)





## Aim of the thesis & thesis outline

The aim of the thesis is to analyze the fluid dynamic models of wind energy conversion systems, pointing out the limitations of current engineering models and proposing innovative solutions from the design point of view

The research activities have been divided in two main parts, following the different rotor – flow interaction characteristics:

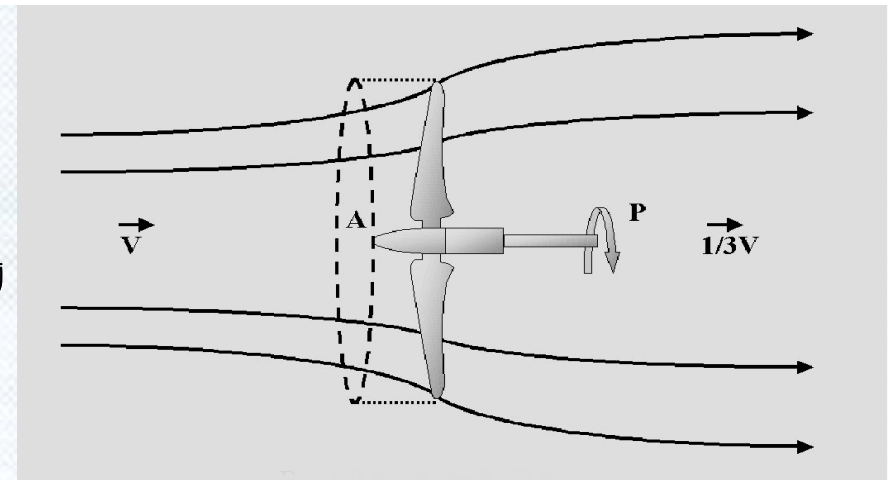
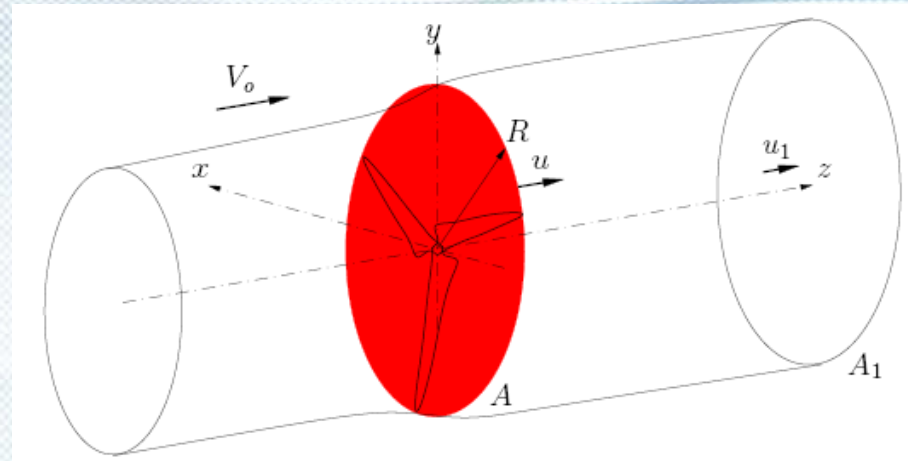
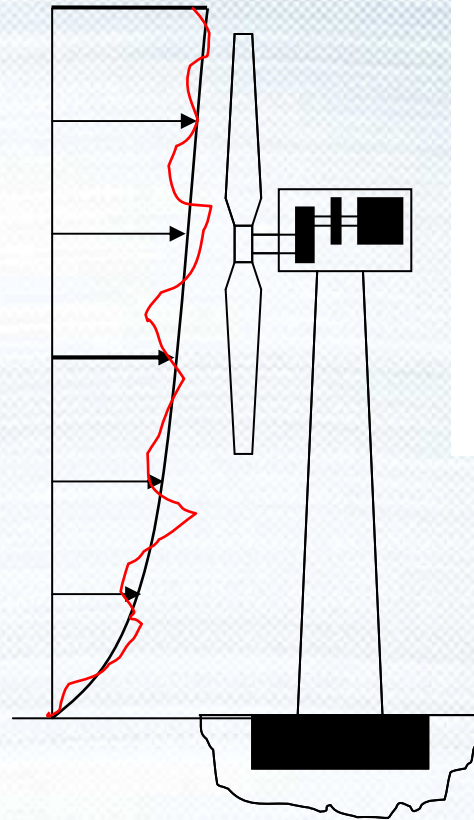
1. Horizontal axis wind turbines - HAWT;
2. Crossflow wind turbines, as vertical axis wind turbines - VAWT.



# Part I : HAWT analysis

## HAWT fluid dynamics

HAWT fluid dynamics is mainly based on the actuator disk concept





# HAWT fluid dynamics

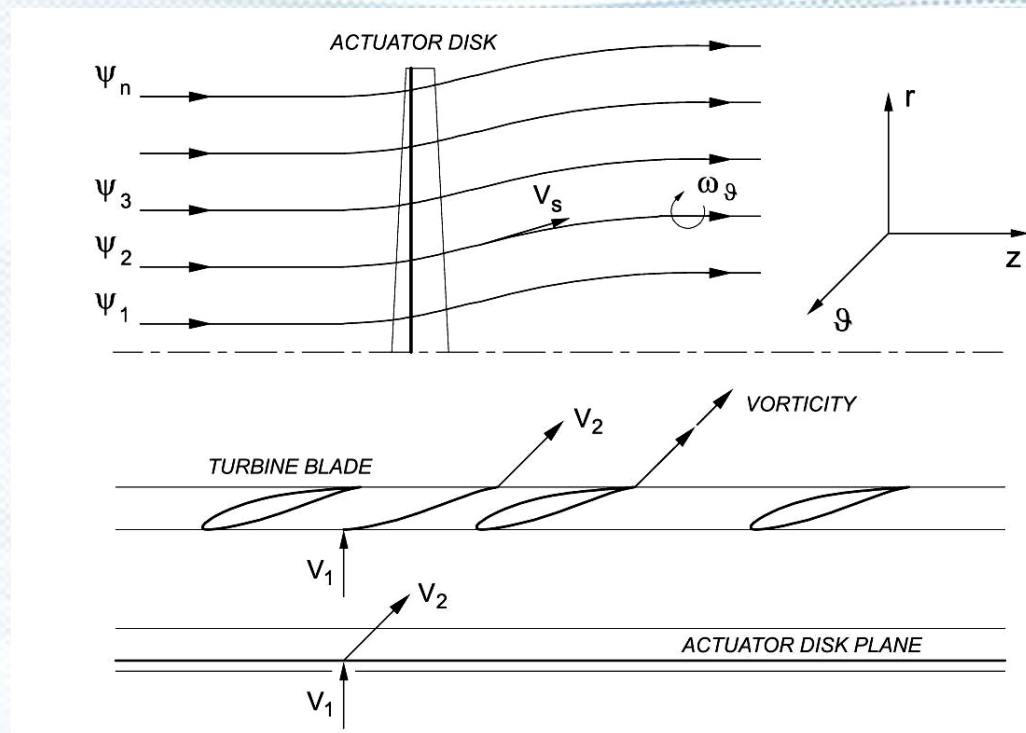
## Actuator disk concept

The turbine generates mechanical work from the kinetic energy of the fluid flow

The work exchange between the fluid and the shaft is done by the rotor, which can be modelled as an actuator disk

The bladed rotor can be represented with equivalent forces distributed over a permeable, immaterial disk

Infinite number of blades  
Infinite rotational velocity





# HAWT fluid dynamics

## Actuator disk – momentum theory

Froude applied for the first time the actuator disk concept to a rotor in open flow.

He applied it with the 1D momentum balance in axial direction

Momentum equation

$$T = \Delta p \cdot A_m = \rho V_{z,3} A_3 (V_{z,0} - V_{z,3})$$

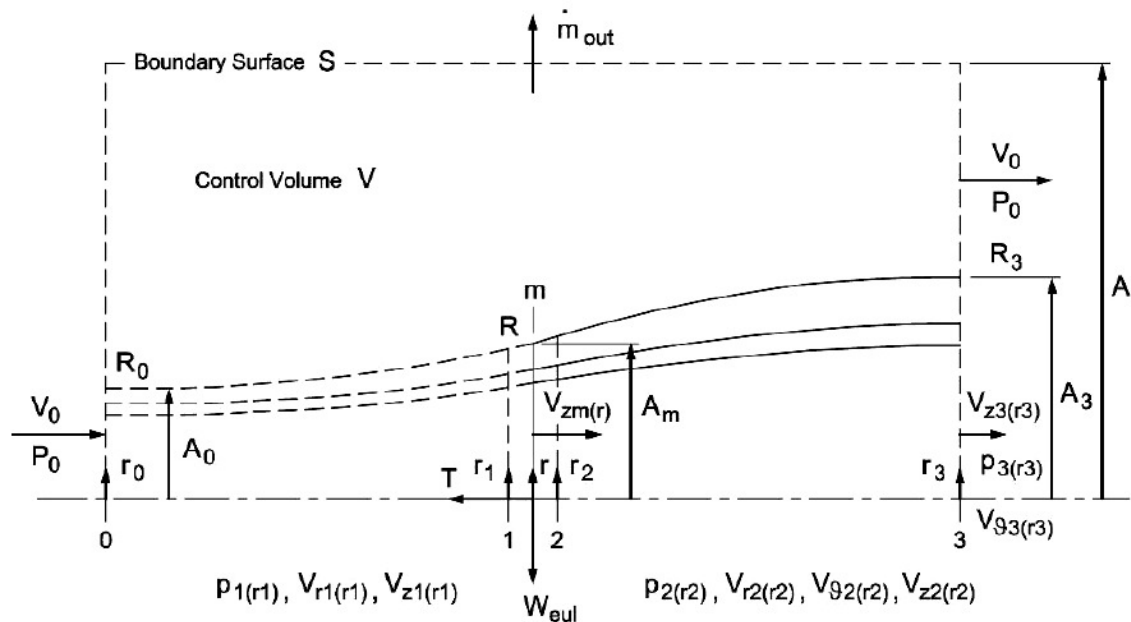
Energy conservation

$$W_{eul} = \frac{\Delta p}{\rho} = \frac{V_{z,0}^2 - V_{z,3}^2}{2}$$

Mass conservation

$$V_{z,m} A_m = V_{z,3} A_3$$

$$V_{z,1} \cong V_{z,2} \cong V_{z,m}$$



Froude result!

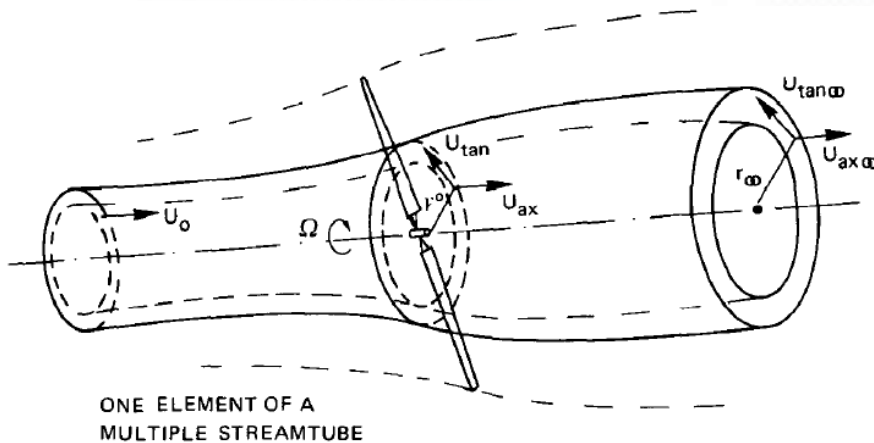
$$V_{z,m} = \frac{V_{z,0} + V_{z,3}}{2}$$





# Actuator disk

## Blade element – momentum theory

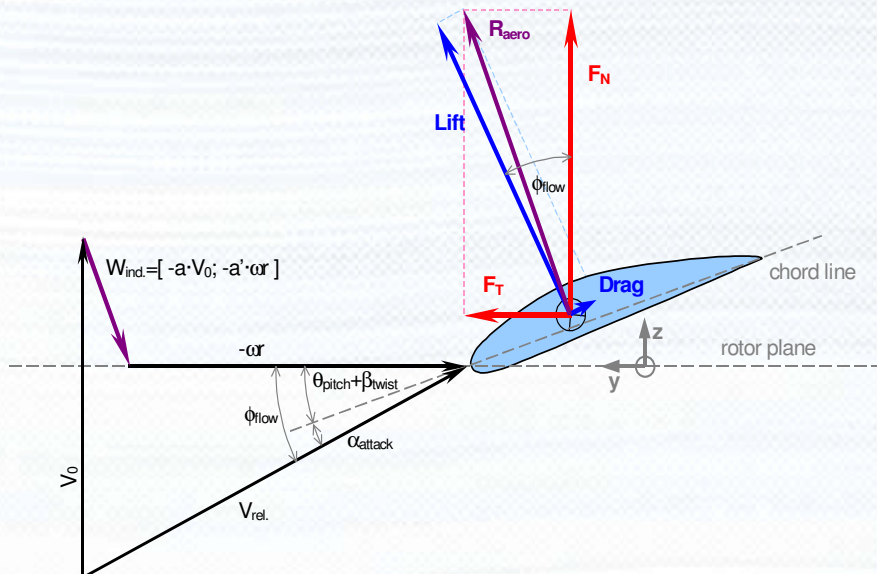


Drzewiecki first applied Froude result dividing the rotor in different annular streamtubes :  
Non uniform loading

$$V_{z,m} = \frac{V_{z,0} + V_{z,3}}{2}$$

With the blade element airfoil theory rotor performances can be easily calculated

The annuli interaction is neglected  
No swirl flow, (wake expansion?)  
Ok lightly loaded rotors





# HAWT fluid dynamics

## General momentum theory

The general momentum theory should overcome the issues of the swirl flow modelling

Momentum equation : axial

$$T = \int_{A_m} (p_1 - p_2) dA = \int_{A_3} [\rho V_{z,3} (V_{z,0} - V_{z,3}) + (p_0 - p_3)] dA$$

tangential

$$M = \int_{A_3} \rho V_{\theta,3} V_{z,3} r_3 dA$$

radial

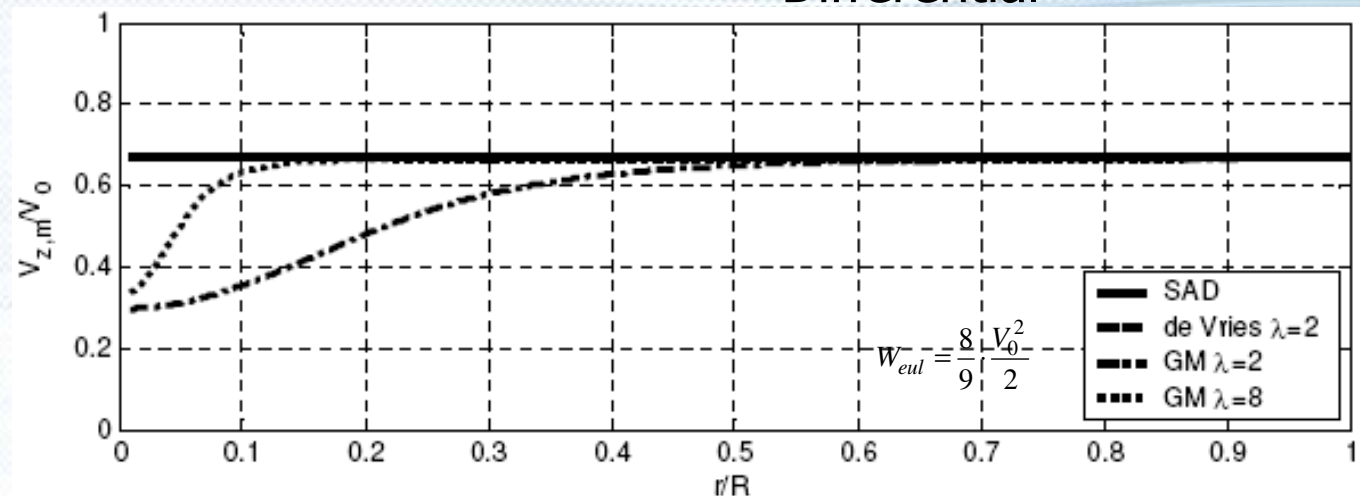
$$\frac{p_3 - p_0}{\rho} = \frac{p_3(r_3) - p_3(r_{tip,3})}{\rho} = - \int_{r_3}^{r_{tip,3}} \frac{V_{\theta,3}^2}{\tilde{r}_3} d\tilde{r}_3$$

$$\frac{1}{2} \rho \int_{A_3} (V_{z,0} - V_{z,3})^2 dA = \rho \Omega \int_{A_3} V_{z,3} V_{\theta,3} r_3 \left[ \frac{1 + 1/2 V_{\theta,3} / \Omega r_3}{V_{z,3}} - \frac{1 + 1/2 V_{\theta,2} / \Omega r}{V_{z,m}} \right] dA$$

Solutions:

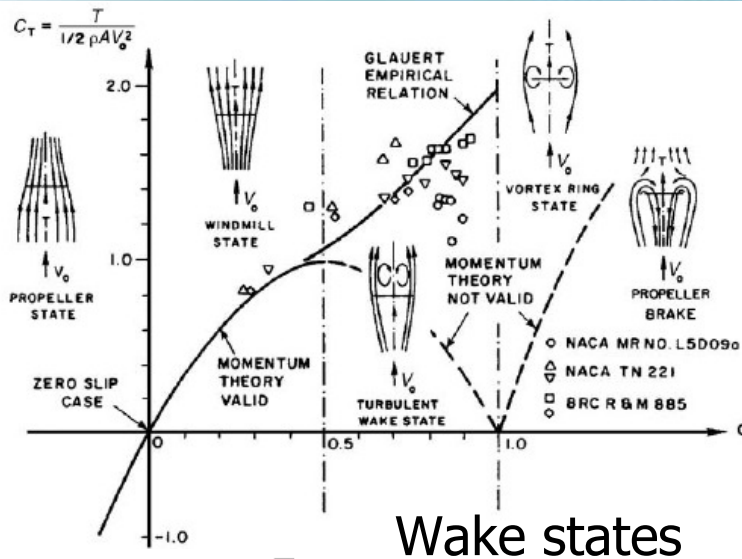
- De Vries
- Differential

- GM theory is an integral formulation
- It needs the wake solution

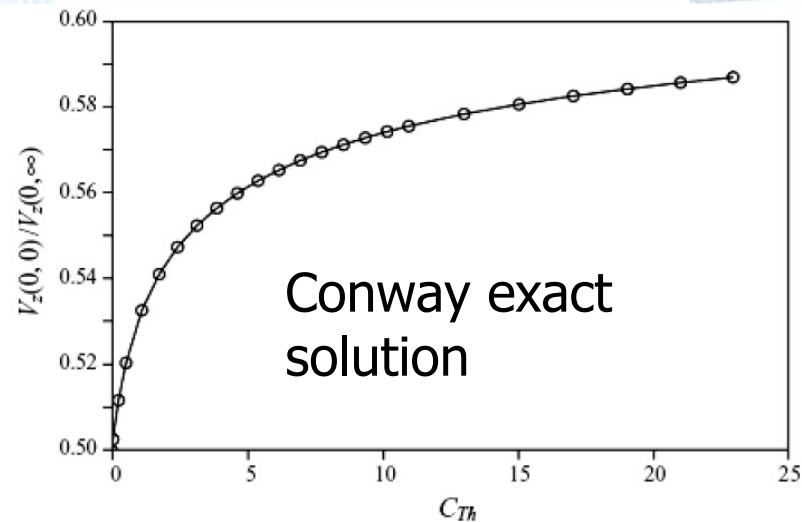
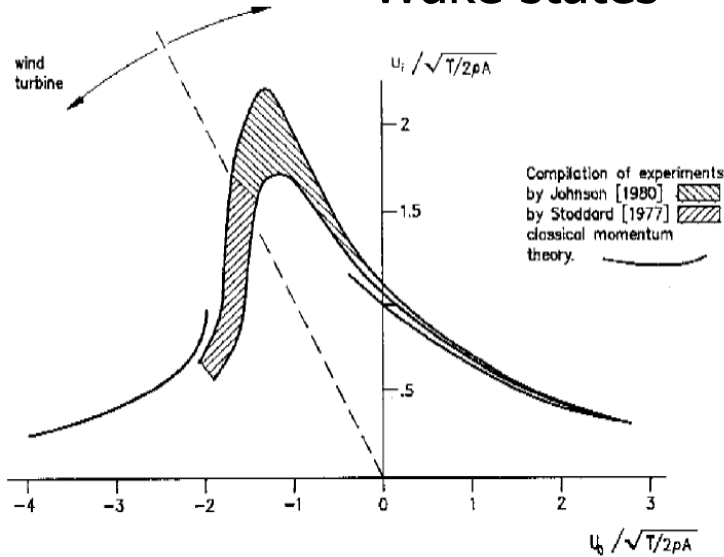
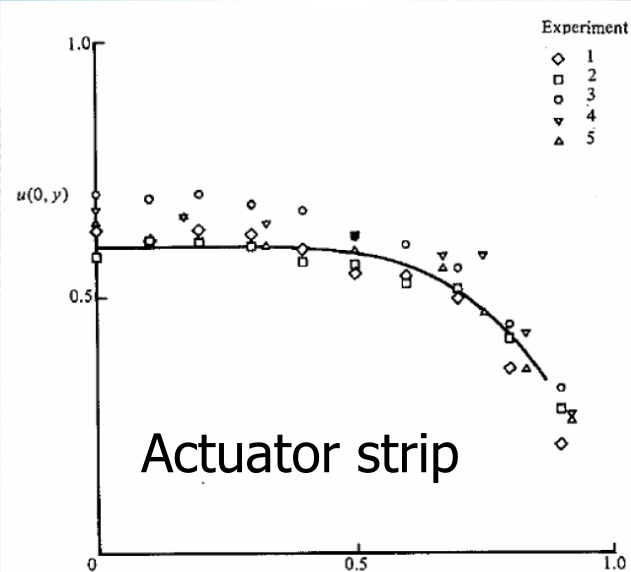




# Actuator disk – momentum theory limitations



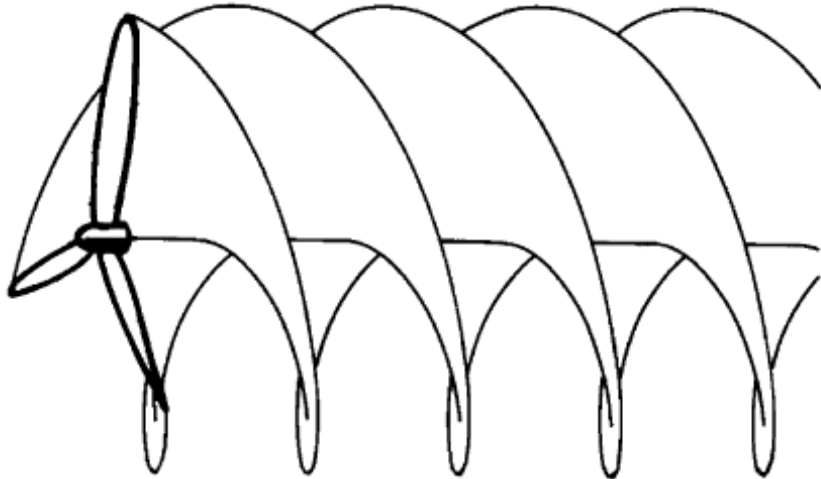
Wake states





# HAWT fluid dynamics

## Vortex theory



Vortex theory calculates the flow field of the rotor wake by using the fluid dynamic laws of vorticity (Biot-Savart law, Kelvin's theorem, Helmholtz's laws)

Introduced by Joukowski – Betz – Prandtl

Most widespread for propeller analysis and design (both for aerodynamic and marine propellers) and for helicopter rotor performance prediction

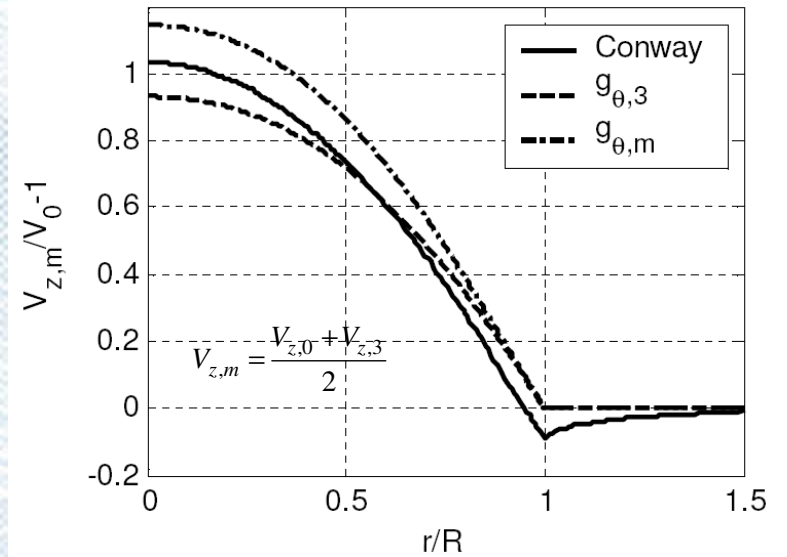
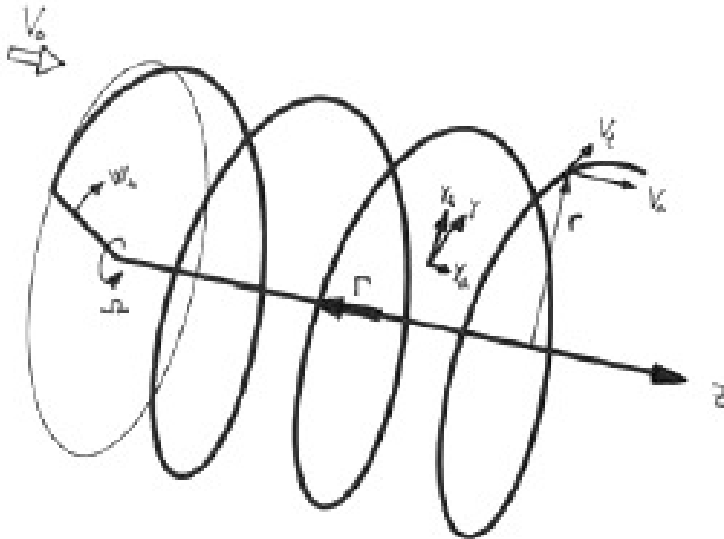
- Prescribed vortex wake
- Free vortex wake





# Vortex theory

## Prescribed vortex wake



Axial velocity

$$d\Gamma = 2\pi \cdot d(rV_{\theta,2})$$

$$g_{\theta,m} = \frac{d\Gamma}{2\pi r} \frac{r\Omega + V_{\theta,2}/2}{V_{z,m}}$$

$$g_{\theta,3} = \frac{d\Gamma}{2\pi r_3} \frac{r_3\Omega + V_{\theta,3}}{V_{z,3}}$$

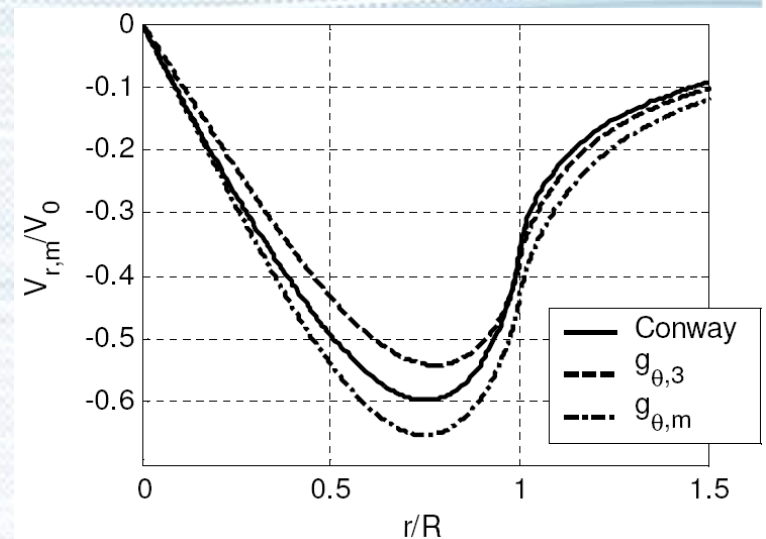
$$v_{z,m} = g_{\theta}/2 \quad v_{z,3} = g_{\theta}$$

Radial velocity

$$V_r(r,0) = -\frac{1}{r} \int_0^r \tilde{r} \frac{\partial V_z}{\partial z}(\tilde{r},0) d\tilde{r}$$

$$\frac{\partial V_z}{\partial z}(\tilde{r},0) = \frac{g_{\theta}}{2r} + \frac{g_{\theta}}{2\pi(r-\tilde{r})} \tilde{r}$$

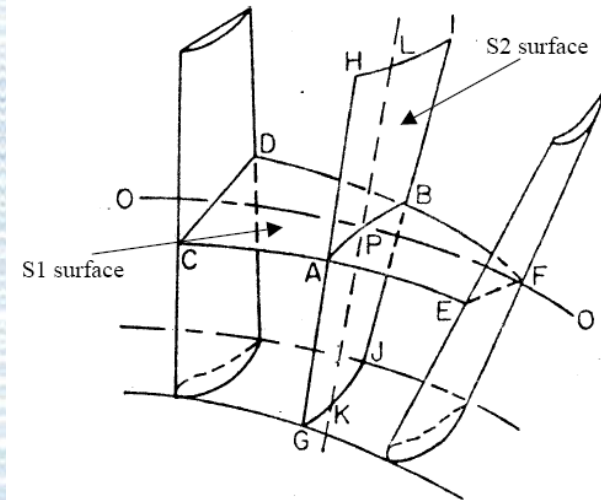
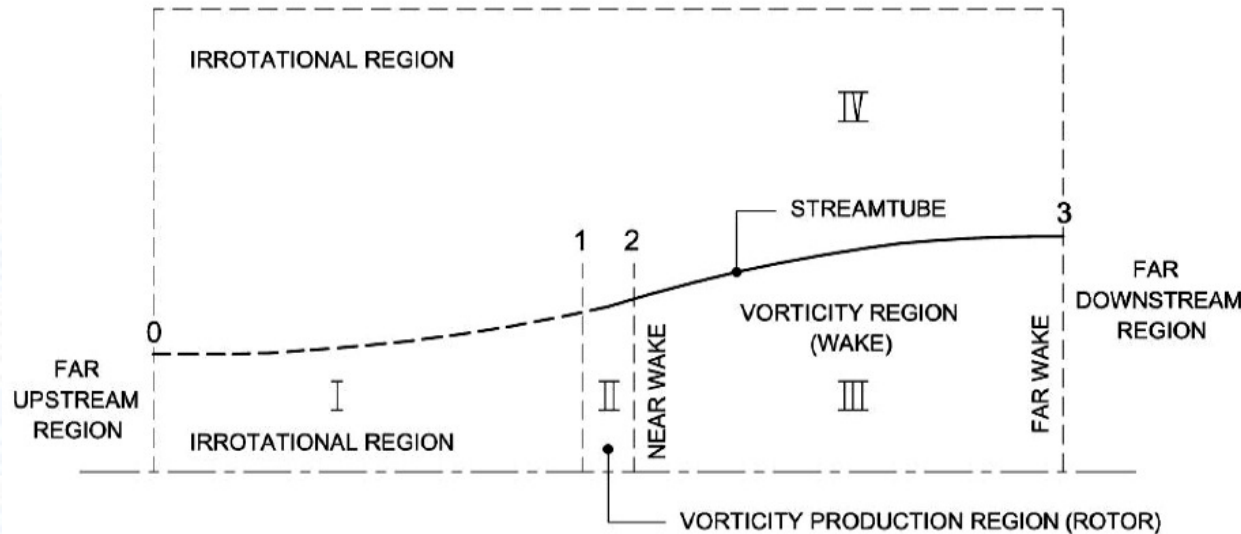
$$\frac{\partial V_z}{\partial z}(\tilde{r},0) = \frac{g_{\theta}}{2\pi(r-\tilde{r})\tilde{r}^2} - \left(\frac{1}{4} - \frac{1}{2\pi}\right) \frac{g_{\theta}(r-\tilde{r})^2}{\tilde{r}^5}$$





# Part I : HAWT analysis

## A turbomachinery approach

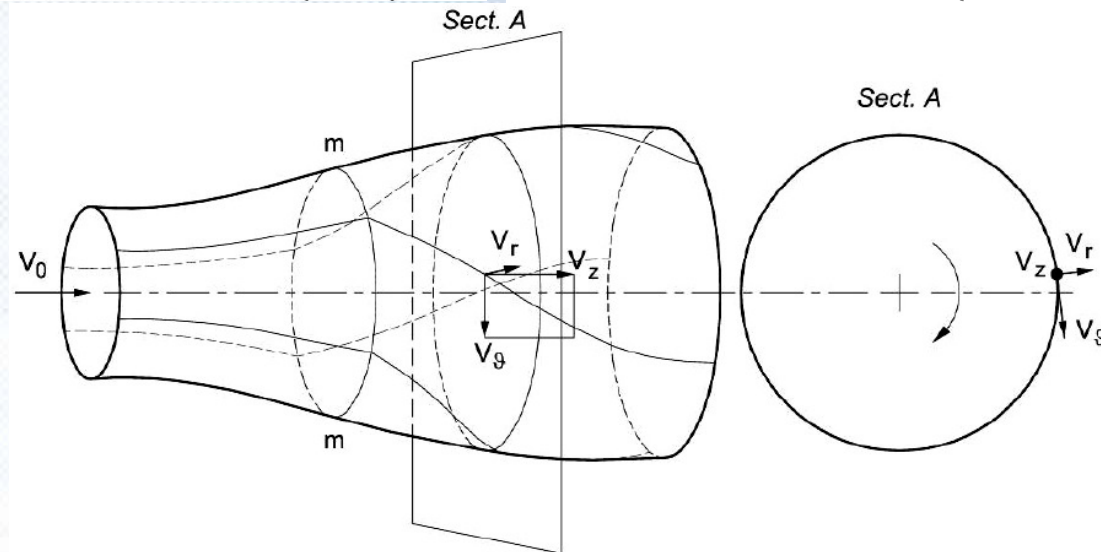


$$\frac{1}{\rho} \frac{\partial p^0}{\partial r} = F_r + \frac{V_\theta}{r} \frac{\partial r V_\theta}{\partial r} - V_z \left( \frac{\partial V_r}{\partial z} - \frac{\partial V_z}{\partial r} \right)$$

$$V_z \frac{\partial V_\theta}{\partial z} + \frac{V_r}{r} \frac{\partial r V_\theta}{\partial r} = F_\theta$$

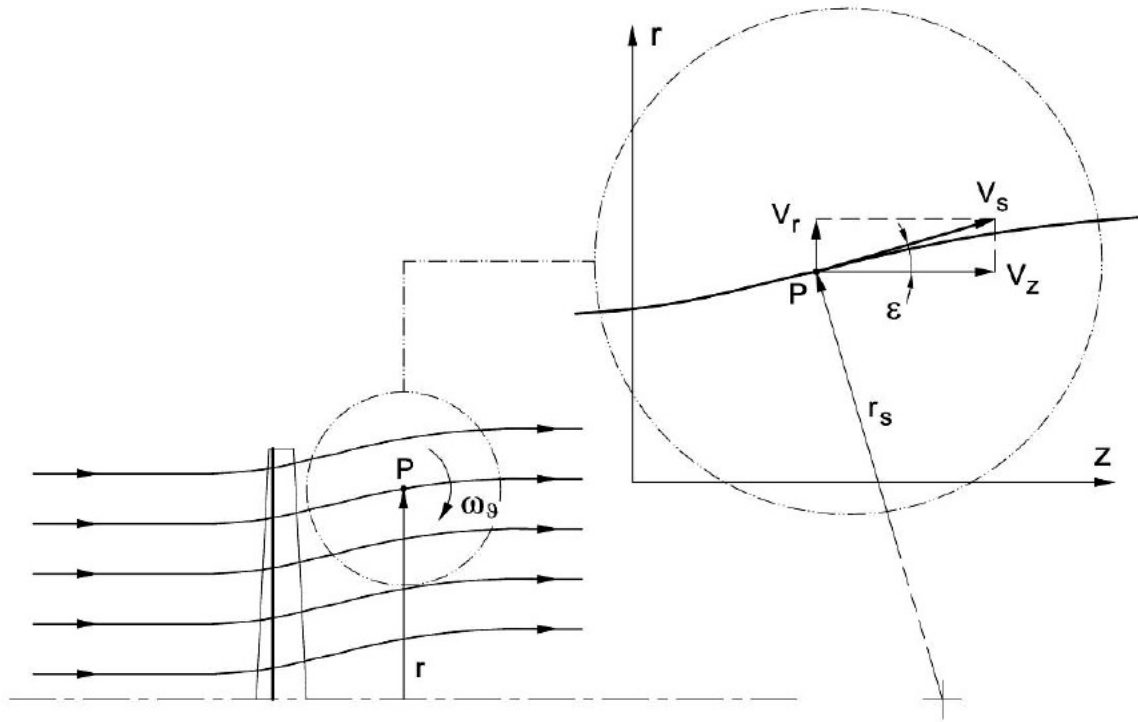
$$\frac{1}{\rho} \frac{\partial p^0}{\partial z} = F_z + V_r \left( \frac{\partial V_r}{\partial z} - \frac{\partial V_z}{\partial r} \right) + V_\theta \frac{\partial V_\theta}{\partial z}$$

$$\frac{\partial r V_r}{\partial r} + \frac{\partial r V_z}{\partial z} = 0$$





# A turbomachinery approach Stoke's stream function



$$\omega_\theta = \frac{\partial V_r}{\partial z} - \frac{\partial V_z}{\partial r}$$

$$\frac{\partial^2 \psi}{\partial r^2} - \frac{1}{r} \frac{\partial \psi}{\partial r} + \frac{\partial^2 \psi}{\partial z^2} = -r \omega_\theta$$

$$\omega_\theta = V_\theta \frac{d(rV_\theta)}{d\psi} - \frac{r}{\rho} \frac{dp^0}{d\psi}$$

$$\frac{\partial^2 \psi}{\partial r^2} - \frac{1}{r} \frac{\partial \psi}{\partial r} + \frac{\partial^2 \psi}{\partial z^2} = 0$$

$$\frac{\partial^2 \psi}{\partial r^2} - \frac{1}{r} \frac{\partial \psi}{\partial r} + \frac{\partial^2 \psi}{\partial z^2} = -r \omega_\theta = -r V_\theta \frac{d(rV_\theta)}{d\psi} + \frac{r^2}{\rho} \frac{dp^0}{d\psi}$$

Linearized solution : Horlock actuator disk solution

$$\frac{\partial^2 \psi}{\partial r^2} - \frac{1}{r} \frac{\partial \psi}{\partial r} + \frac{\partial^2 \psi}{\partial z^2} = -F(r)$$

$$V_z(r, z) = V_{z,0} + \left( \frac{V_{z,3} - V_{z,0}}{2} \right) e^{kz}$$

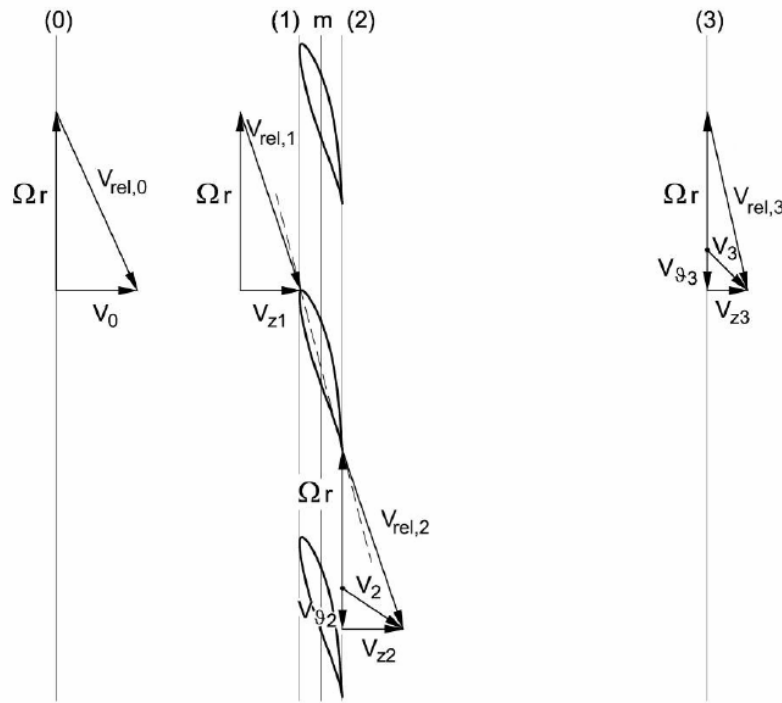
$$V_r(r, z) = -\frac{1}{r} \int_0^r k \tilde{r} \left( \frac{V_{z,3}(\tilde{r}) - V_{z,0}}{2} \right) e^{kz} d\tilde{r}$$

Froude result



# A turbomachinery approach

## Motion in region II



The angular momentum distribution can be assigned

$$V_{\theta} = k_1 r^n + \frac{k_2}{r}$$

$$rV_{\theta} = k_1 r^{n+1} + k_2$$

The flow is determined by

$$rV_{\theta} \quad p^0$$

Euler equation

$$\frac{1}{\rho} (p_2^0 - p_1^0) = \Omega r V_{\theta} = W_{eul}$$

Wu equation

$$\frac{\partial^2 \psi}{\partial r^2} - \frac{1}{r} \frac{\partial \psi}{\partial r} + \frac{\partial^2 \psi}{\partial z^2} = \left[ -\frac{(p_2^0 - p_1^0)/\rho}{\Omega^2} + r^2 \right] \frac{1}{\rho} \frac{dp_2^0}{d\psi} = (\Omega r^2 - rV_{\theta}) \frac{d(rV_{\theta})}{d\psi}$$

Free vortex distribution

$$rV_{\theta} = const$$





# The radial equilibrium theory applied to wind turbines

## Radial momentum equilibrium

$$\frac{1}{\rho} \frac{\partial p^0}{\partial r} = F_r + \frac{V_\theta}{r} \frac{\partial r V_\theta}{\partial r} - V_z \left( \frac{\partial V_r}{\partial z} - \frac{\partial V_z}{\partial r} \right)$$

$$\frac{1}{\rho} \frac{dp^0}{dr} = \frac{V_\theta}{r} \frac{d(rV_\theta)}{dr} + V_z \frac{dV_z}{dr} \quad \text{ISRE}$$

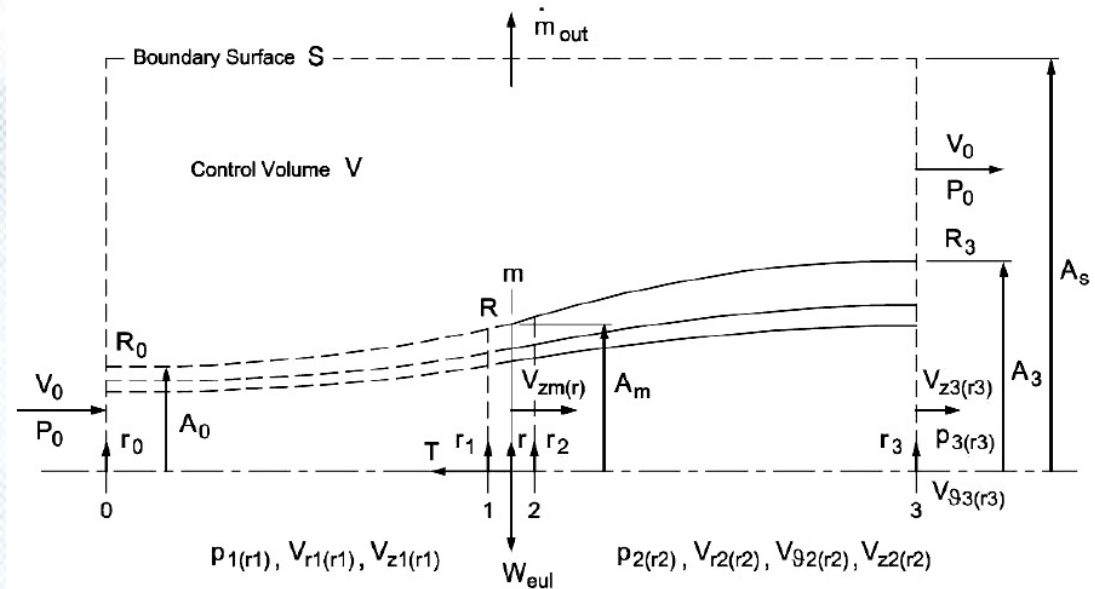
## Sections 1 - 2

$$V_z^2 - V_{z,hub}^2 = \frac{2}{\rho} (p^0 - p_{r,hub}^0) - 2 \int_{r,hub}^r \frac{V_\theta}{\tilde{r}} \frac{\partial r V_\theta}{\partial r} d\tilde{r} + 2 \int_{r,hub}^r V_z \left( \frac{\partial V_r}{\partial z} \right)_\psi d\tilde{r} - (V_r^2 - V_{r,hub}^2)$$

## Wu hypothesis

$$\frac{\partial V_{r,1}}{\partial z} = - \frac{\partial V_{r,2}}{\partial z}$$

$$\frac{1}{\rho} \frac{dp_2^0}{dr} = \frac{V_{\theta,2}}{r} \frac{d(rV_{\theta,2})}{dr} + 2V_{z,m} \frac{dV_{z,m}}{dr}$$



## Wu hypothesis on a streamline

$$\left( \frac{\partial V_{r,1}}{\partial z} \right)_\psi = - \left( \frac{\partial V_{r,2}}{\partial z} \right)_\psi$$

$$\frac{1}{\rho} \frac{dp_2^0}{dr} = \frac{V_{\theta,2}}{r} \frac{d(rV_{\theta,2})}{dr} + 2V_{z,m} \frac{dV_{z,m}}{dr} + 2V_{r,m} \frac{dV_{r,m}}{dr}$$

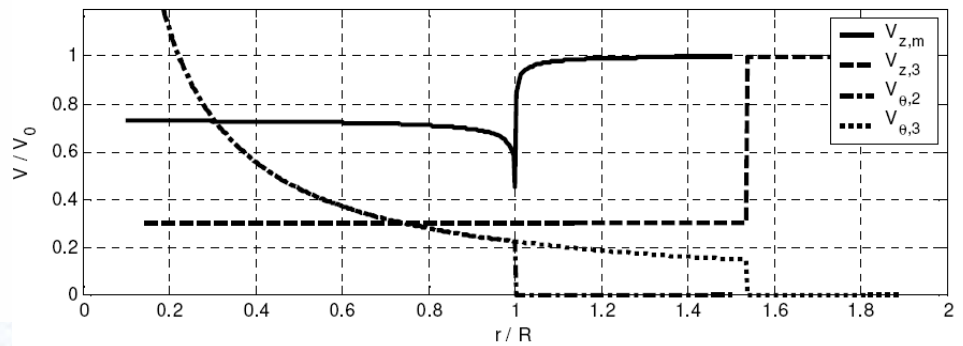
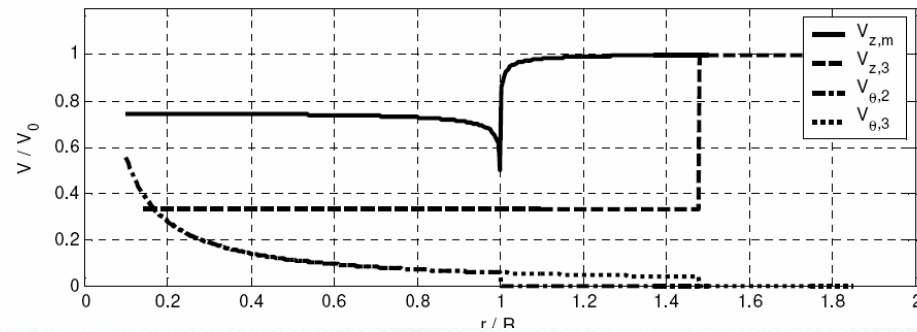
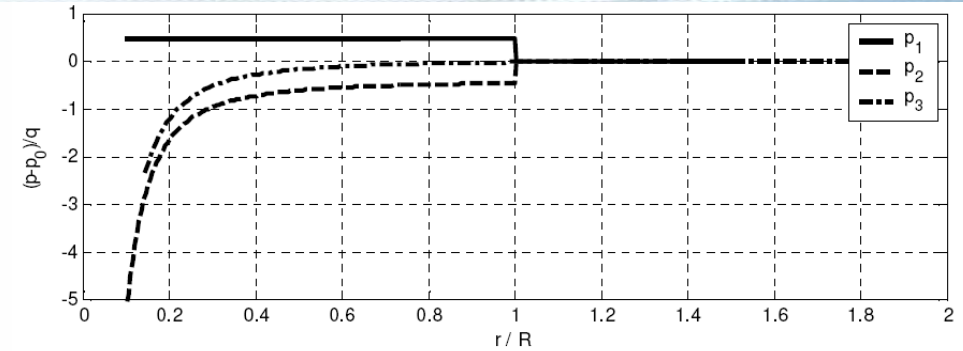
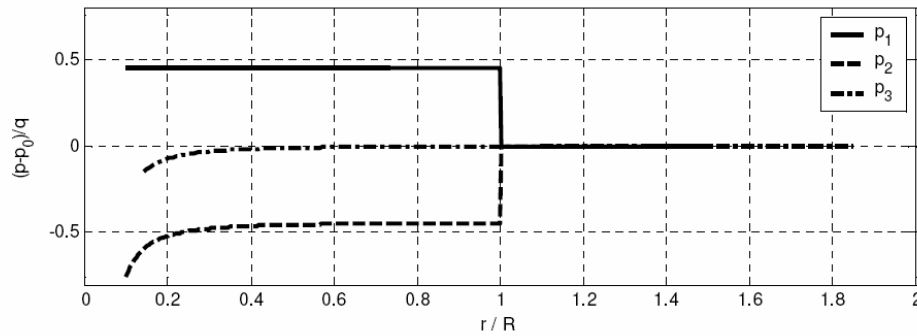


# The radial equilibrium theory results and comments

Radial equilibrium solution for a uniformly loaded disk

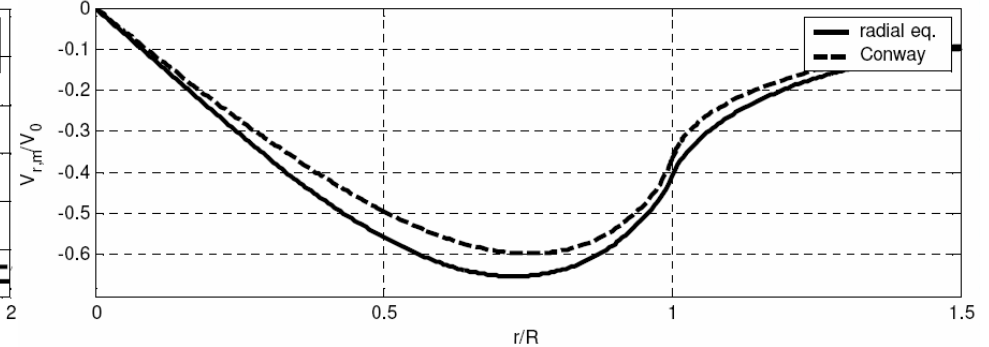
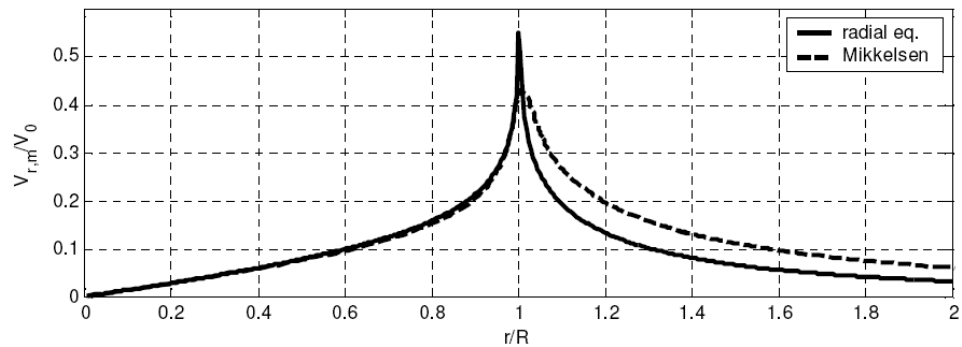
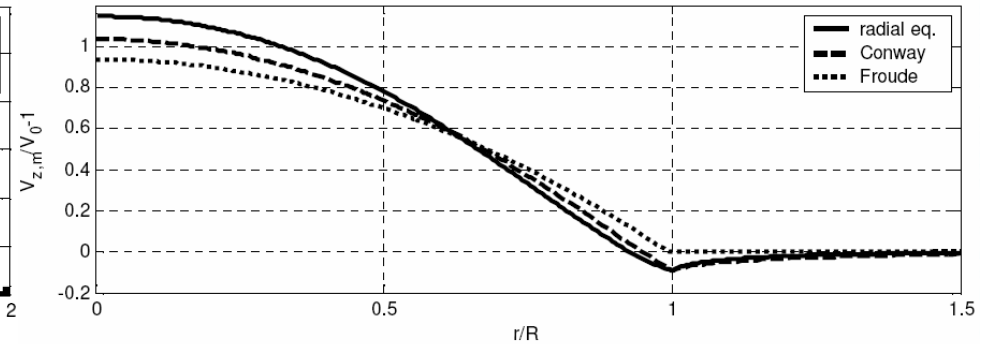
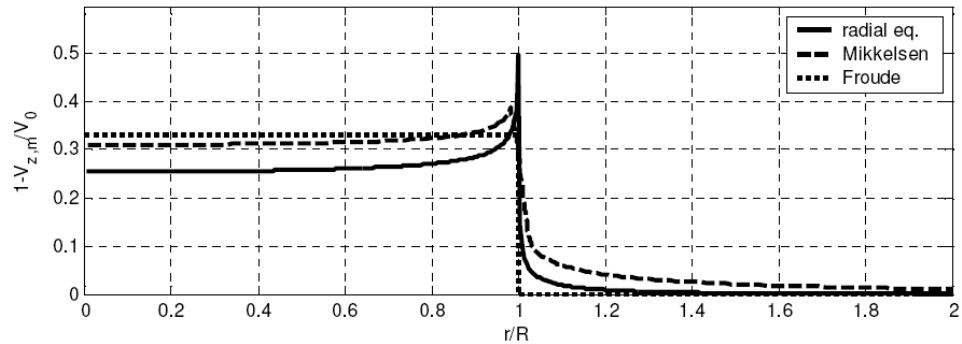
$$\lambda = 8 \quad W_{eul} = \frac{8}{9} \cdot \frac{V_0^2}{2}$$

$$\lambda = 2 \quad W_{eul} = \frac{8}{9} \cdot \frac{V_0^2}{2}$$





# The radial equilibrium theory results and comments



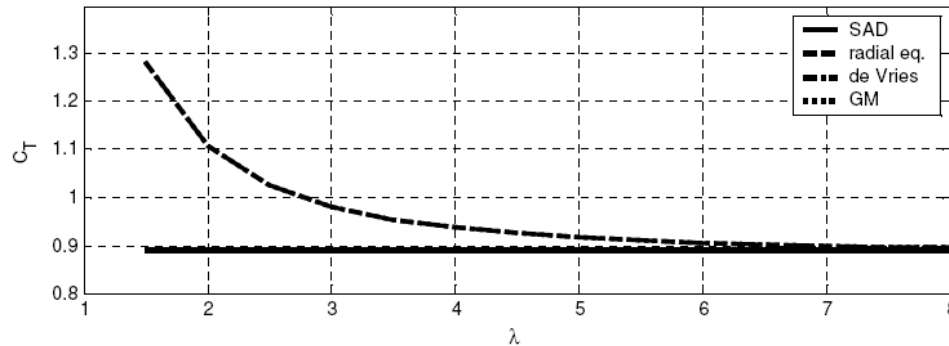
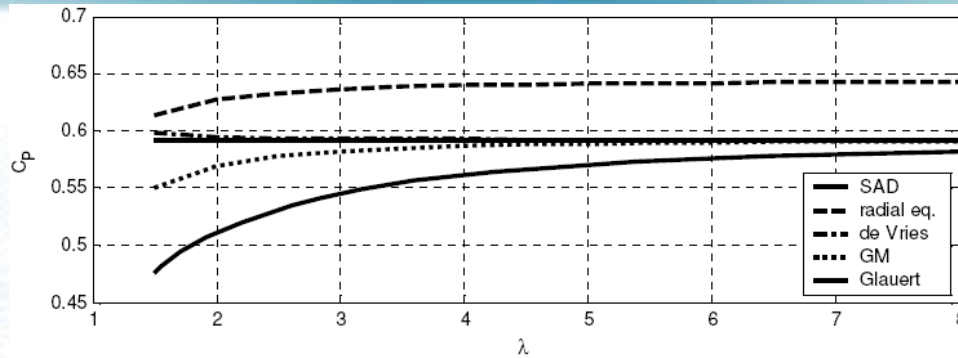
Mikkelsen actuator disk – CFD solution for a uniformly highly loaded disk (wind turbine state)

$$W_{eul} = \frac{8}{9} \cdot \frac{V_0^2}{2}$$

Conway actuator disk – vortex theory exact solution for a (almost) parabolic highly loaded disk (propeller state)  $C_T = 3.147$

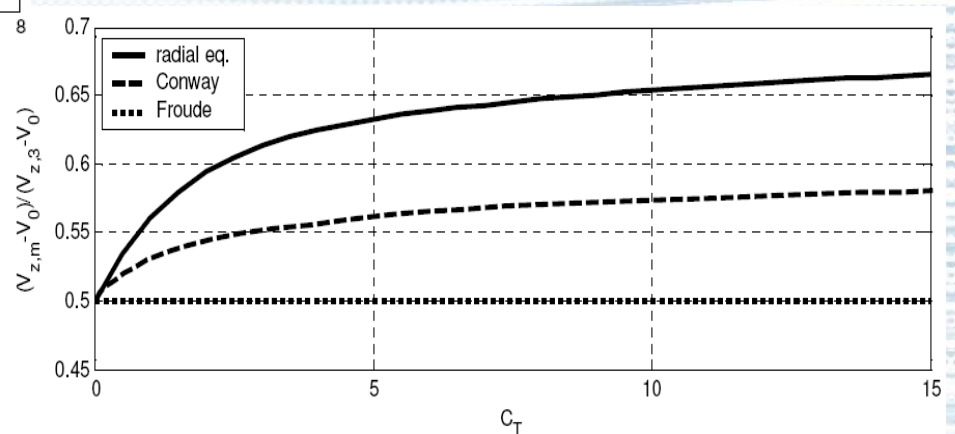


# The radial equilibrium theory results and comments



Conway velocity at the centre of the disk for a propeller

Power and thrust coefficients for the different flow field solution models with a constant work extraction





# The radial equilibrium theory on a streamline

## Radial equilibrium with meridional velocity

$$\frac{1}{\rho} \frac{dp_2^0}{dr} = \frac{V_{\theta,2}}{r} \frac{d(rV_{\theta,2})}{dr} + 2V_{s,m} \frac{dV_{s,m}}{dr}$$

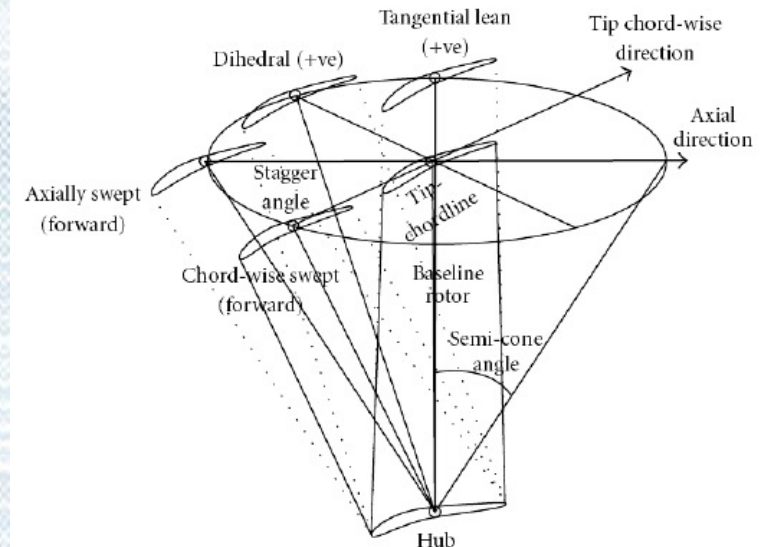
$$V_{s,m}^2 = V_{z,m}^2 + V_{r,m}^2$$

## Denton / Cumpsty approach

$$\frac{1}{2} \frac{\partial V_s^2}{\partial q} = \frac{1}{\rho} \frac{\partial p^0}{\partial q} + V_s \frac{\partial V_s}{\partial s} \sin(\varepsilon + \delta) + \frac{V_s^2}{r_s} \cos(\varepsilon + \delta) - \frac{1}{2r^2} \frac{\partial}{\partial q} (r^2 V_\theta^2) + \frac{V_s}{r} \frac{\partial}{\partial s} (r V_\theta) \tan \gamma + F_d$$

$$\frac{1}{2} \frac{\partial V_s^2}{\partial r} = \frac{1}{\rho} \frac{\partial p^0}{\partial r} + V_s \frac{\partial V_s}{\partial s} \sin \varepsilon - \frac{V_s^2}{r_s} \cos \varepsilon - \frac{1}{2r^2} \frac{\partial}{\partial q} (r^2 V_\theta^2)$$

$$\frac{\partial V_{s,m}^2}{\partial r} = \frac{1}{\rho} \frac{\partial p_2^0}{\partial r} + 2V_{r,m} \frac{\partial V_{s,m}}{\partial s} - V_{s,m}^2 \cos \varepsilon \left( \frac{1}{r_{s,1}} + \frac{1}{r_{s,2}} \right) - \frac{1}{2r^2} \frac{\partial}{\partial q} (r^2 V_\theta^2)$$



Coning / yaw effects  
Turbulence wake state / stall

Tip effects  
Unsteady dynamics



# Considerations on the turbomachinery approach

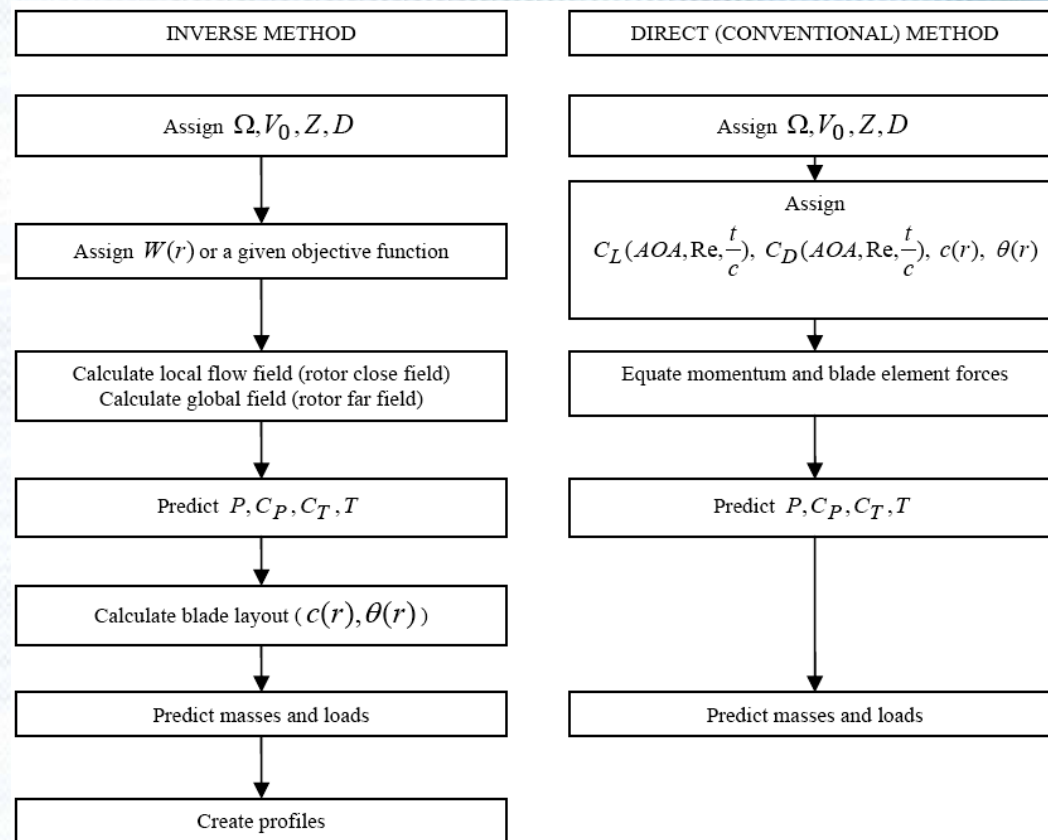
- The theory handles an expanding and rotating wake.
- Only the disk station has to be solved to obtain the information needed to compute  $CP$  and  $CT$ .
- The method is simple and robust also for low tip speed ratios
- Arbitrary disk loading can be analyzed.
- The mathematics involved are comparable with those of the usual actuator disk approaches.
- The actual velocities distribution are qualitatively assessed even though more work has to be carried out to better understand the fluid flow in the neighborhood of the disk and in the wake.
- The radial velocity gradients along the streamlines at the disk have to be better described to reduce the axial velocity overestimation at the disk inner portion.



# Part I : HAWT analysis

## Inverse Design

### Inverse design and direct design methods





# The turbine close field structure

## The blade architecture

### Blade forces

$$F_{\theta,Z} = \rho \cdot V_{z,m} \cdot s \cdot (V_{\theta,2} - V_{\theta,1}) = \rho \cdot V_{z,m}^2 \cdot s \cdot (\tan \alpha_2 - \tan \alpha_1)$$

$$F_{z,Z} = (p_1^0 - p_2^0) \cdot s + \frac{1}{2} \rho \cdot V_{\theta,2}^2 \cdot s$$

$$W_{eul} = U \cdot (V_{\theta,2} - V_{\theta,1}) = U \cdot V_{z,m} \cdot (\tan \alpha_2 - \tan \alpha_1) = U \cdot V_{z,m} \cdot (\tan \beta_2 - \tan \beta_1)$$

$$W_{eul} = r\omega \cdot \left( k_1 r^n + \frac{k_2}{r} \right)$$

### Flow angles

$$\beta_1 = \tan^{-1} \left( \frac{U + V_{\theta,1}}{V_{z,1}} \right) \quad \beta_m = \tan^{-1} \left( \frac{U + V_{\theta,m}}{V_{z,m}} \right) \quad \beta_2 = \tan^{-1} \left( \frac{U + V_{\theta,2}}{V_{z,2}} \right)$$

### The blade architecture

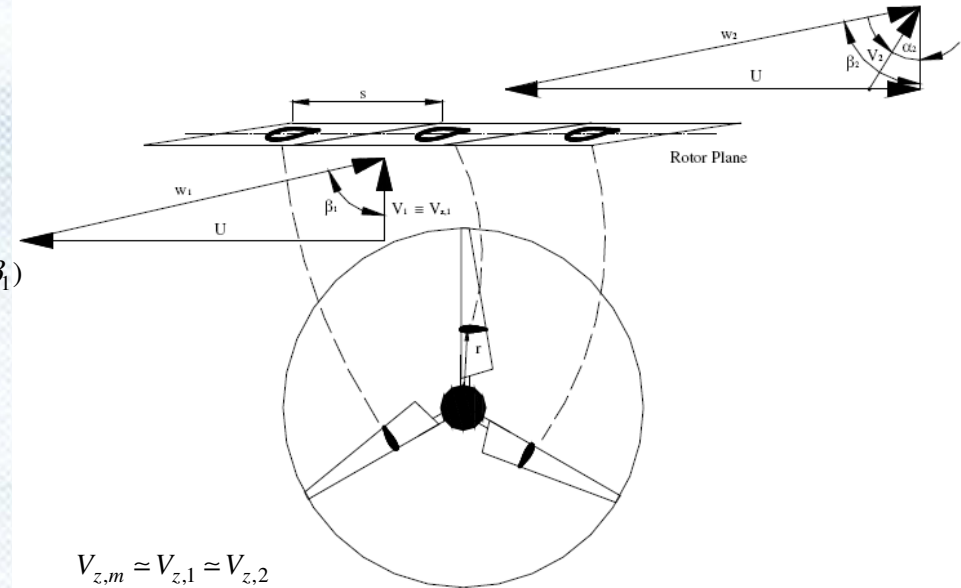
$$C_y = \frac{F_y}{F_{y,max}} = 2 \cdot \frac{s}{c_z} (\tan \beta_2 - \tan \beta_1) \cos^2 \beta_2 \quad c_z = c \cdot \cos \beta_m$$

$$C_y = 0.8$$

Zweifel

$$D_{loc} = \frac{W_{max} - W_2}{W_{max}}$$

Lieblein



$$C_L = 2 \frac{s}{c} (\tan \beta_2 - \tan \beta_1) \cos \beta_m$$

$$\theta = \frac{\pi}{2} - \beta_m - \sin^{-1} \left( \frac{C_{L,ID}}{2\pi} \right)$$



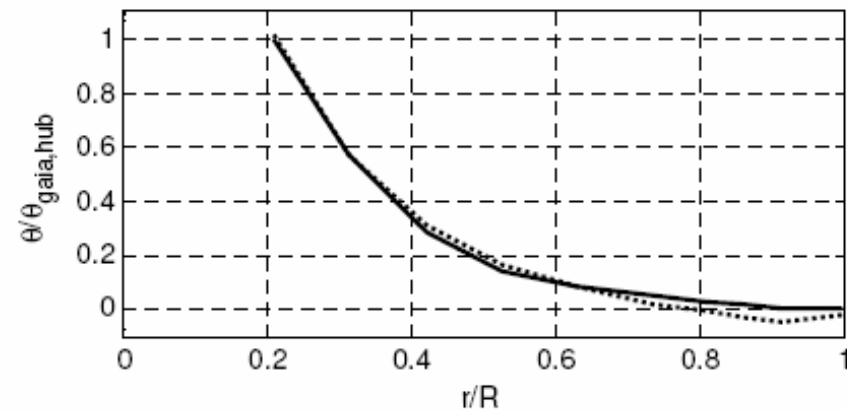
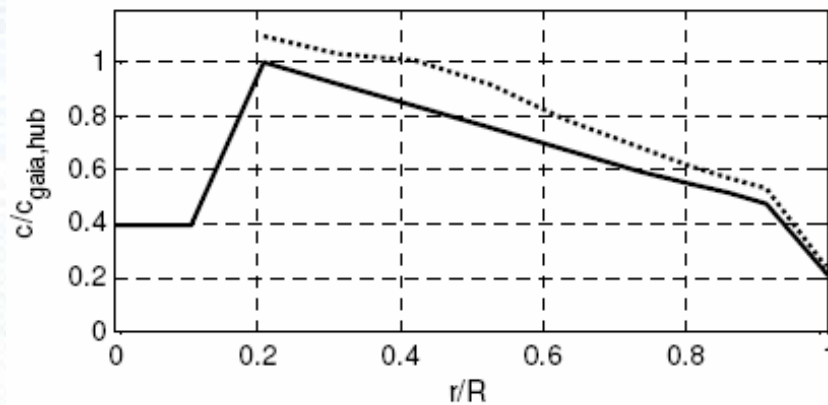


# Inverse Design Results and discussion

Gaia turbine

Table 4-2. Main characteristics of GAIA wind turbine.

Rated power	11 kW
Rotor diameter	13 m
Tower height	18.2 m
Rotors speed	56 rpm

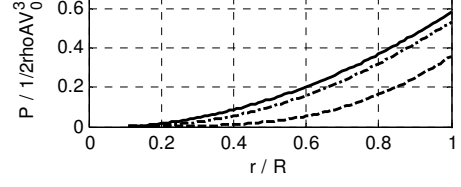
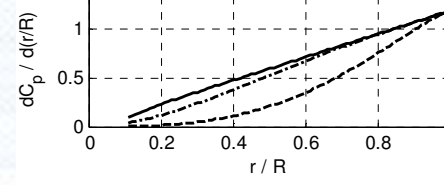
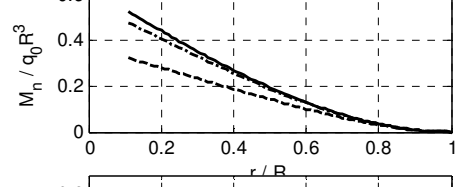
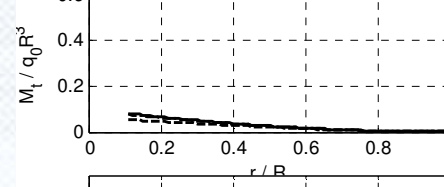
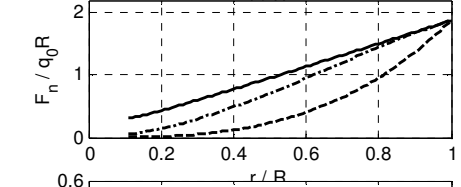
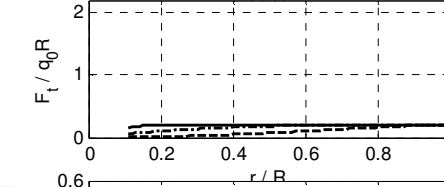
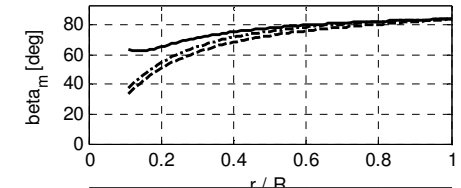
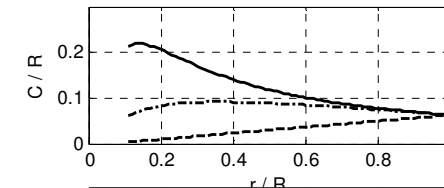
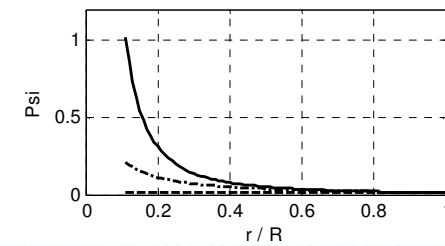
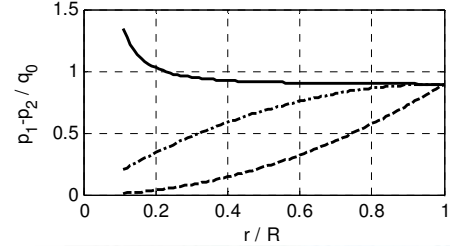
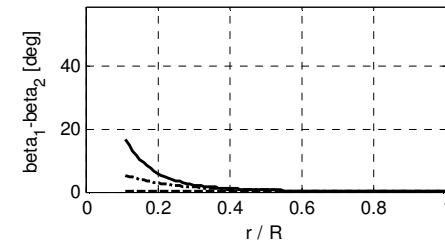
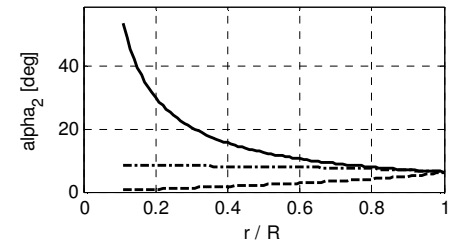
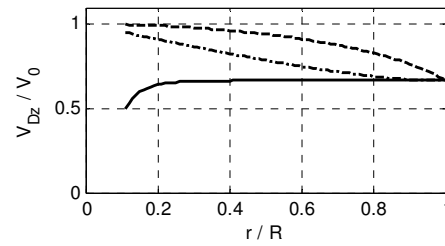
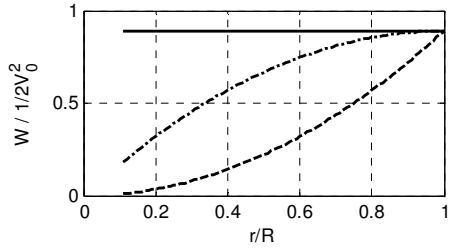




# Inverse Design Results and discussion

Flow characteristics

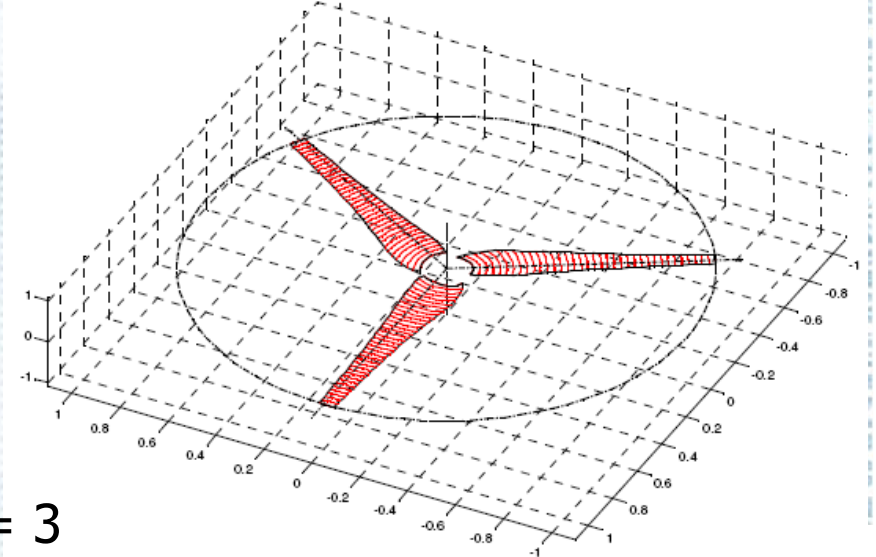
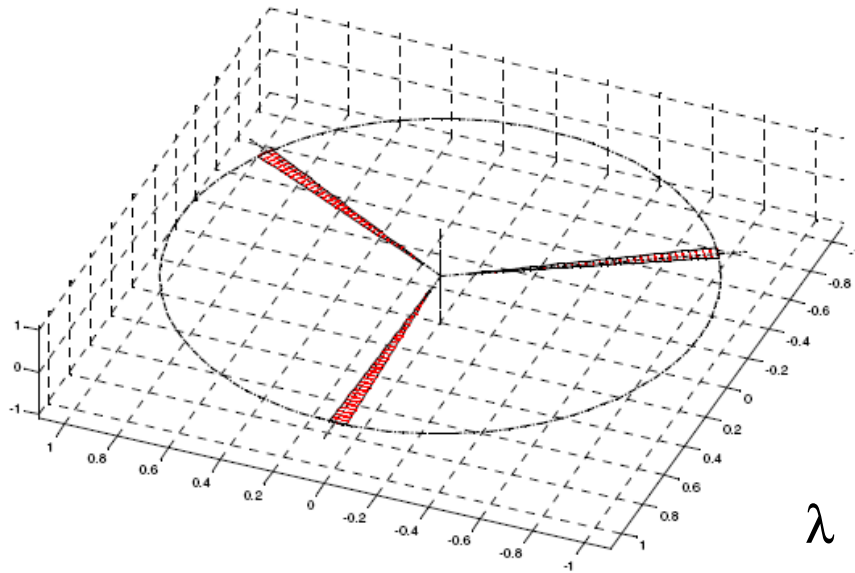
The blade architecture and loads



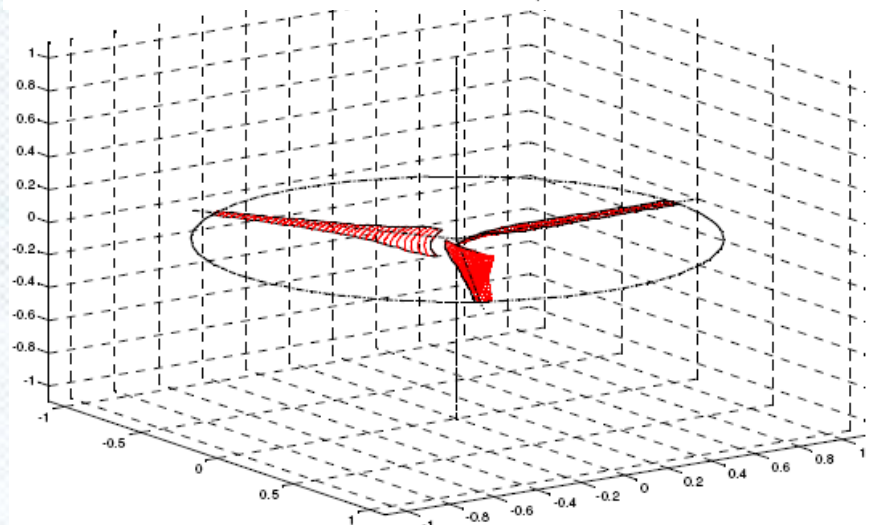
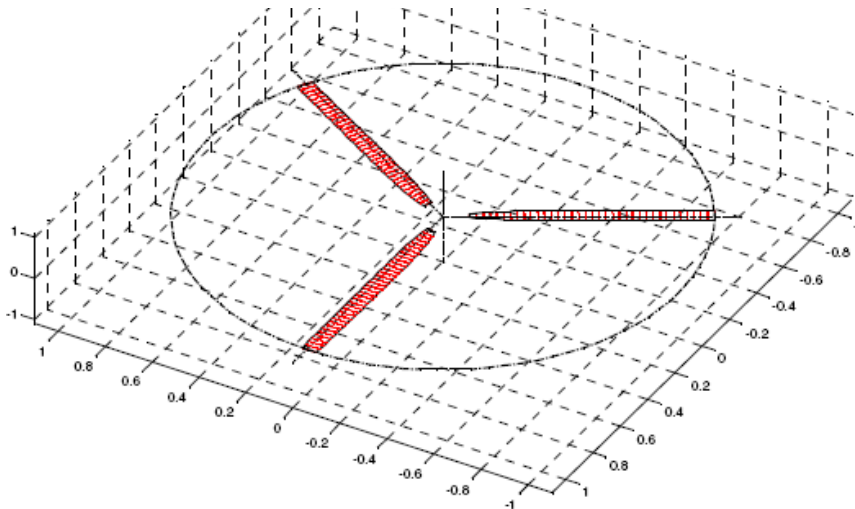
$$\lambda = 6, Z = 3$$



# Inverse Design Results and discussion

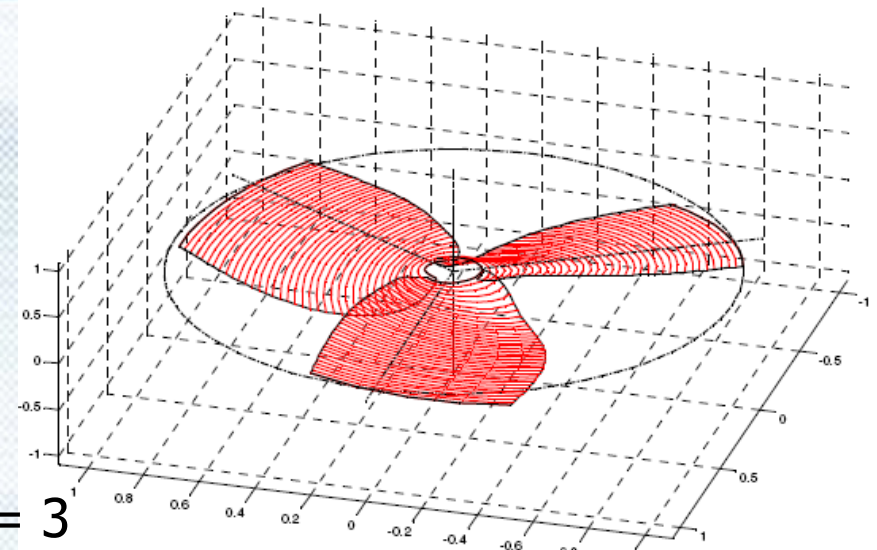
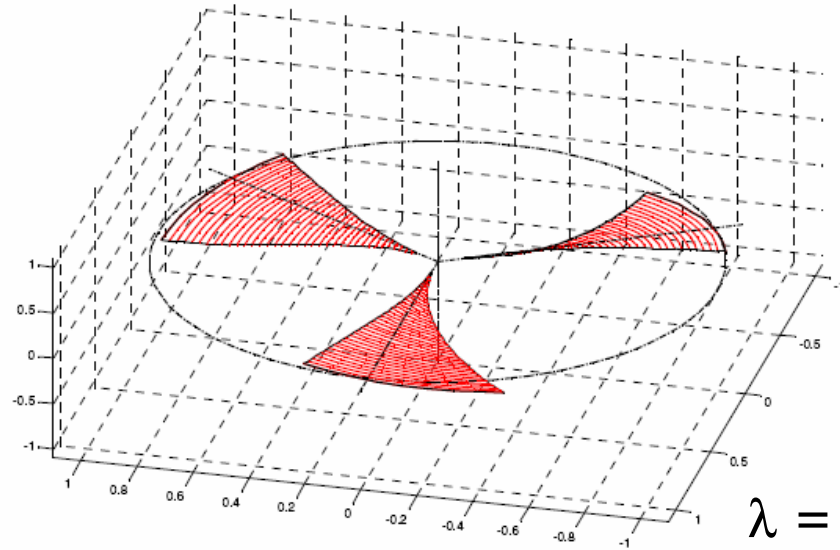


$$\lambda = 6, Z = 3$$

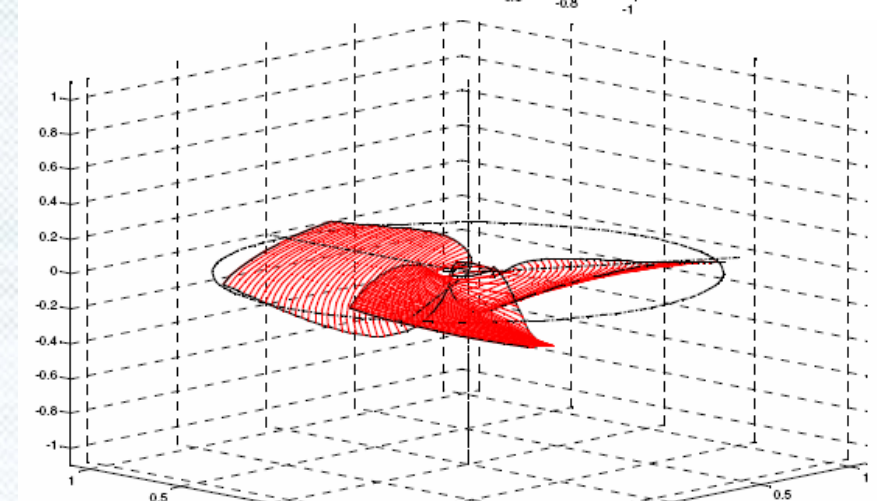
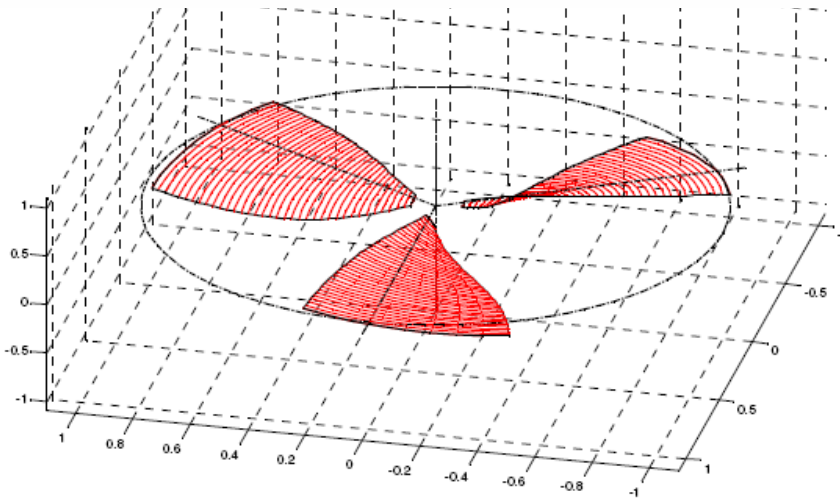




# Inverse Design Results and discussion



$\lambda = 1.5, Z = 3$



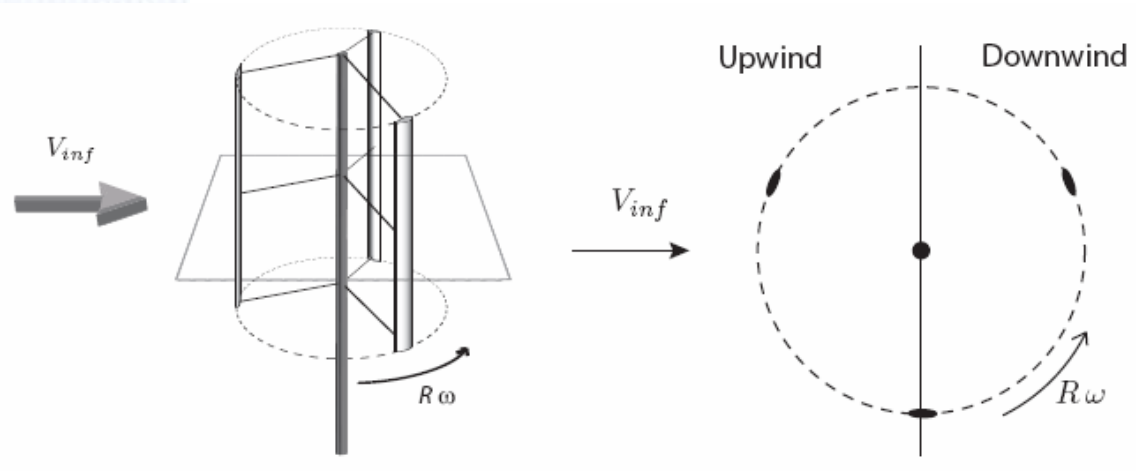
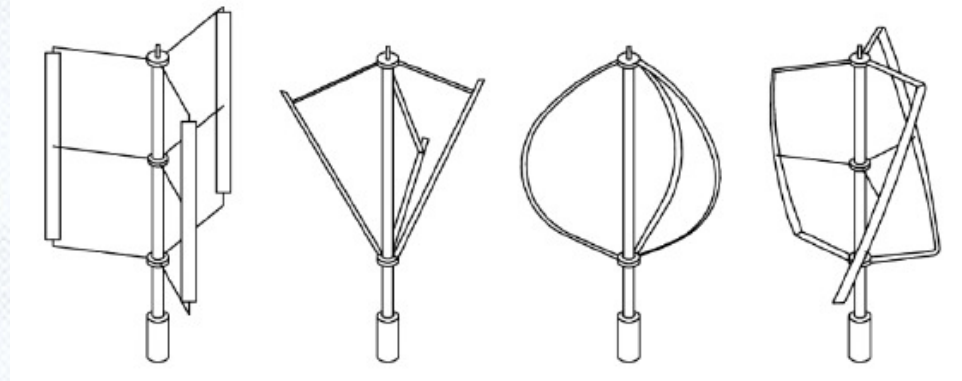


# Part II : VAWT analysis

## VAWT fluid dynamics



Darrieus eggbeater – Darrieus H/V  
– Gorlov type  
Building environment  
Offshore multi Mega Watt





# VAWT fluid dynamics

## The double disk BEM for VAWT

### Flow characteristics

$$\beta = \tan^{-1} \frac{V \sin \vartheta \cos \delta}{(V \cos \vartheta + \Omega r) \cos \gamma}$$

$$W^2 = [(V \cos \vartheta + \Omega r) \cos \gamma]^2 + (V \sin \vartheta \cos \delta)^2$$

$$Re = \frac{cW}{\nu_0}$$

$$C_L = \frac{dL}{\frac{1}{2} \rho_0 W^2 c dh} \quad C_D = \frac{dD}{\frac{1}{2} \rho_0 W^2 c dh}$$

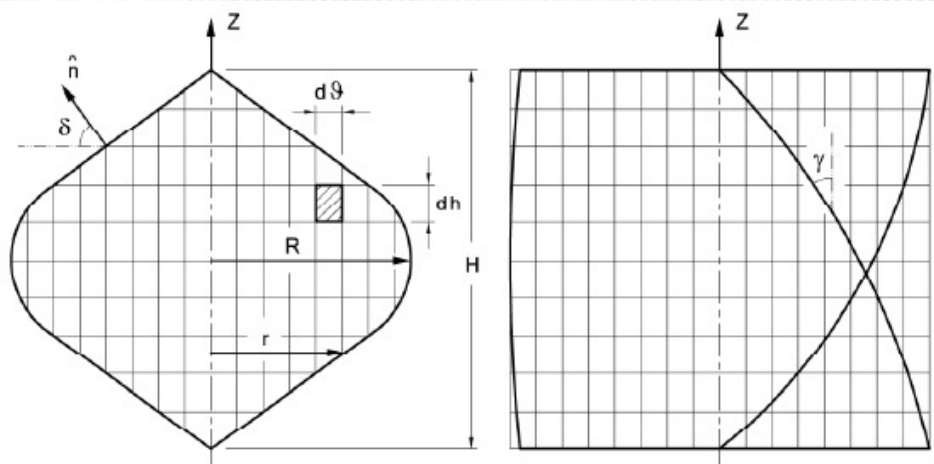
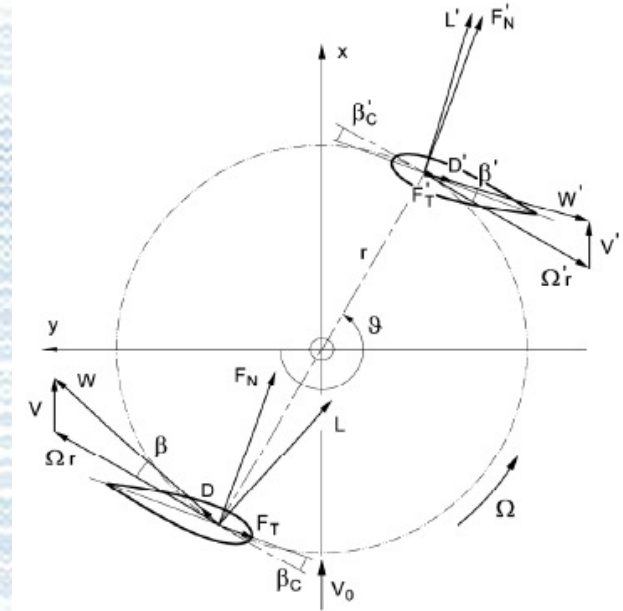
### Blade element forces

$$C_N = C_L \cos \beta + C_D \sin \beta$$

$$C_T = C_L \sin \beta - C_D \cos \beta$$

$$dF_N = \frac{1}{2} \rho_0 W^2 c \frac{dh}{\cos \delta} C_N$$

$$dF_T = \frac{1}{2} \rho_0 W^2 c \frac{dh}{\cos \delta} C_T$$



### Shaft torque/power

$$dM = dF_T \Omega$$

$$C_P = \frac{\bar{M} \Omega}{\frac{1}{2} \rho_0 A_{sw} V_0^3} = \frac{1}{N_\vartheta} \int \int \int dM \Omega$$



# VAWT fluid dynamics

## The double disk BEM for VAWT

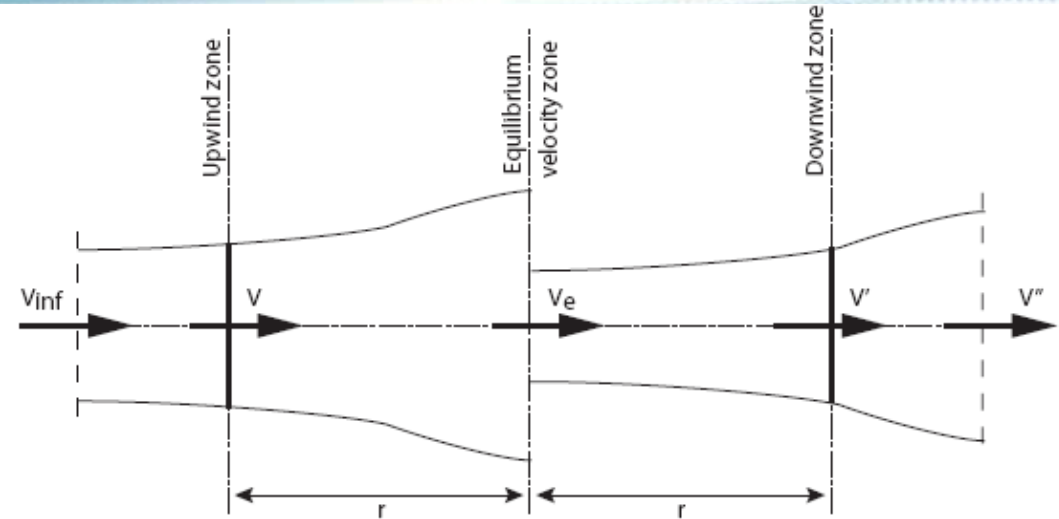
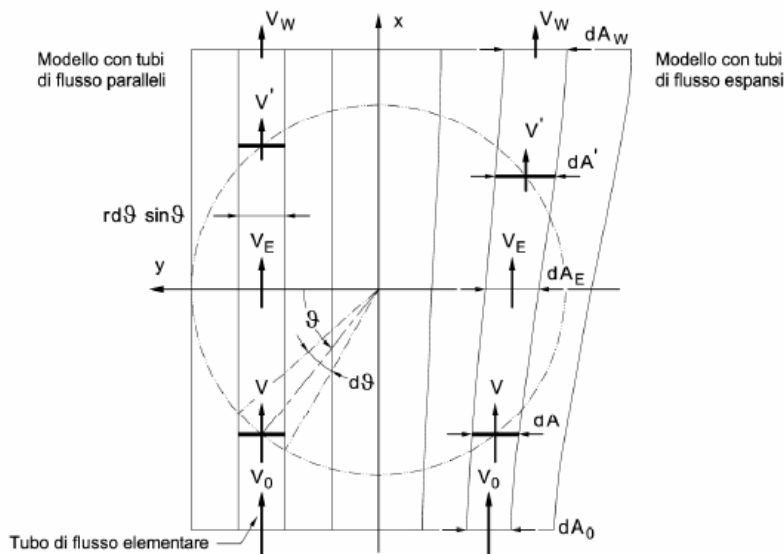
### Blade element

$$dF_x = dF_T \cos \vartheta \cos \beta_c \cos \gamma + dF_N \sin \vartheta \cos \delta$$

$$\overline{dF_x} = B 2 \frac{\Delta \vartheta}{\pi} dF_x$$

$$C_{TH} = \frac{\overline{dF_x}}{\frac{1}{2} \rho_0 V_0^2 dA_s}$$

$$dA_s = dh r d\vartheta \sin \vartheta$$



### Momentum theory

$$\alpha = \frac{V}{V_0}$$

$$dF_x = 2\rho dA_s V(V_0 - V)$$

$$C_{TH} = \frac{dF_x}{\frac{1}{2} \rho V_0^2 dA_s} = \frac{2\rho dA_s V(V_0 - V)}{\frac{1}{2} \rho V_0^2 dA_s} = 4\alpha(1 - \alpha)$$



# The double disk BEM for VAWT Corrections

Glauert correction

$$C_{TH} = \frac{26}{15}(1-\alpha) + \frac{4}{15}$$

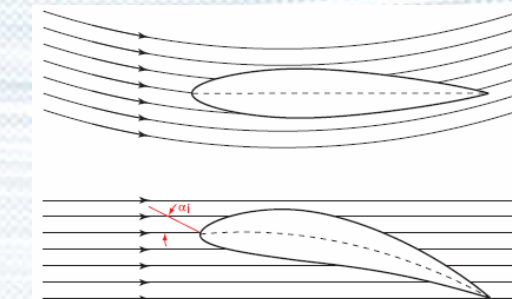
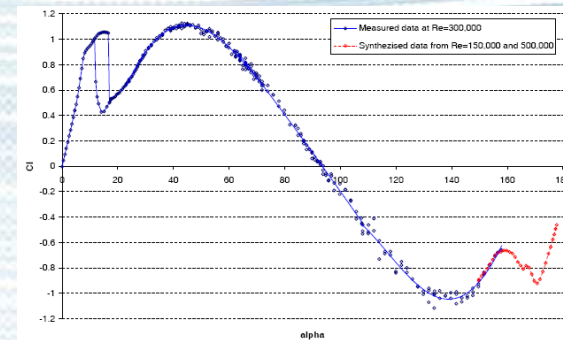
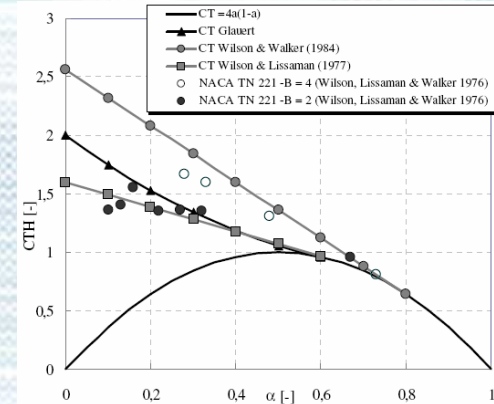
Tip losses

Post stall airfoil performance  
correction

Flow curvature

Dynamic stall

Streamtubes expansion



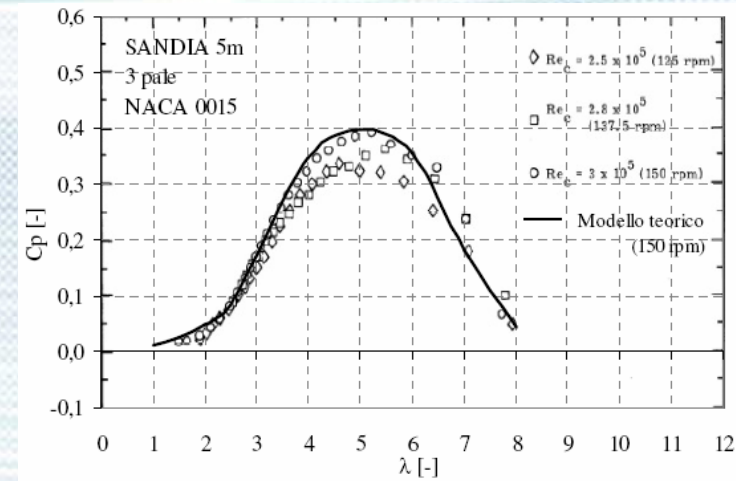




# VAWT fluid dynamics Validation and results

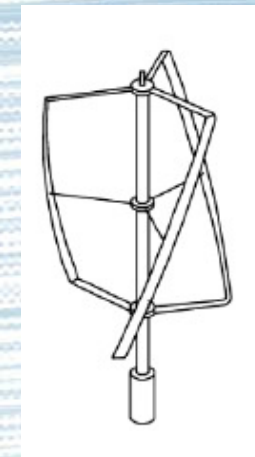
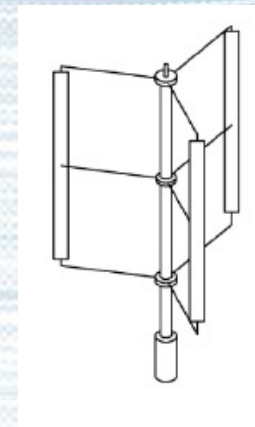
Sandia 5m  
Darrieus  
3 blades  
NACA0015

H	5,1 m
D	5,0 m
c	0,152 m
Airfoil	NACA0015
Solidity	0,1



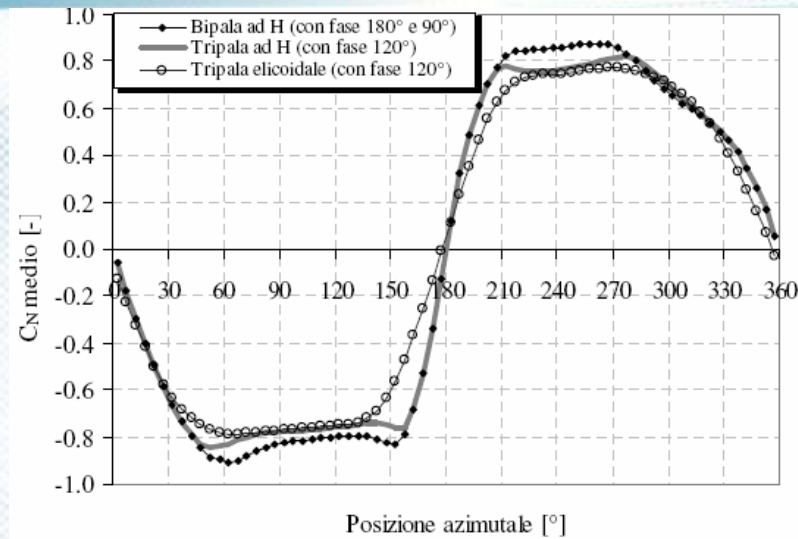
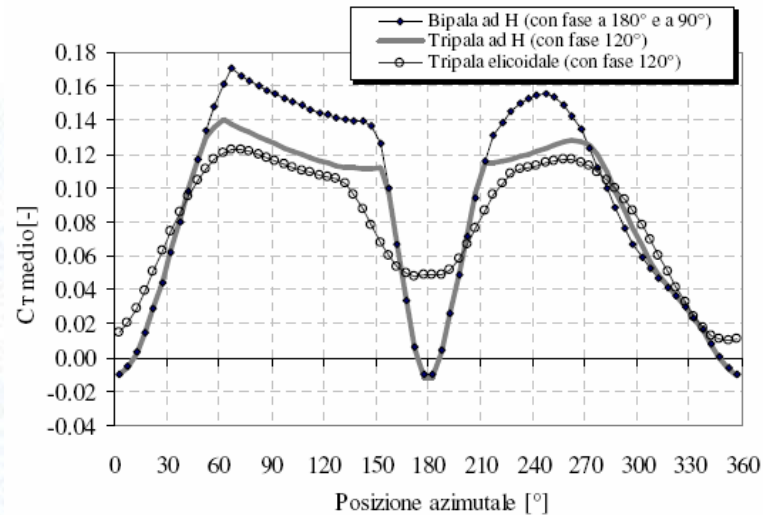
## Four geometric characteristics

	A	B	C	D
H	2,5 m	2,5 m	2,5 m	2,5 m
D	1,8 m	1,8 m	1,8 m	1,8 m
c	0,148 m	0,148 m	0,099 m	0,092 m
Airfoil	NACA0018	NACA0018	NACA0018	NACA0018
Blade geometry	Straight blade ( $\gamma = 0^\circ$ )	Straight blade ( $\gamma = 0^\circ$ )	Straight blade ( $\gamma = 0^\circ$ )	Helicoidal blade ( $\gamma = 20,51^\circ$ )
Blades number	2	2	3	3
Blades spacing	180°	90°	120°	120°
Solidity	0,166	0,166	0,166	0,166





# VAWT fluid dynamics Validation and results



Blade tangential and normal force coefficients

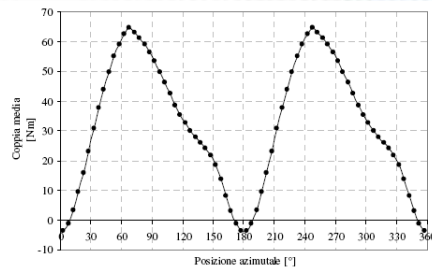
Shaft forces and torque  
Mean value and fluctuations

	A	B	C	D
Torque <sub>mean</sub>	32,14 Nm	32,14 Nm	28,83 Nm (-10%)	27,19 Nm (-15%)
R <sub>Torque</sub>	2,13	0,97 (-54%)	0,57 (-73%)	0,32 (-82%)
F <sub>x mean</sub>	204 N	204 N	194 N (-5%)	193 N (-5%)
R <sub>F<sub>x</sub></sub>	1,80	0,42 (-77%)	0,35 (-80%)	0,35 (-80%)
F <sub>y mean</sub>	-24,4 N	-24,4 N	-20,0 N (-18%)	-16,2 N (-34%)
R <sub>F<sub>y</sub></sub>	-19,5	-9,3 (-52%)	-4,7 (-76%)	-3,9 (-80%)
$R = \frac{Value_{max} - Value_{min}}{Value_{mean}}$				

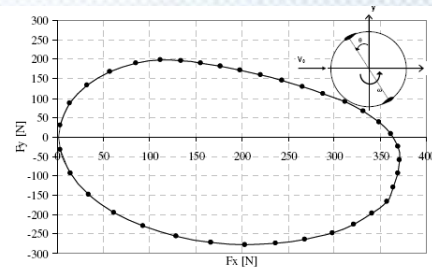


# VAWT fluid dynamics Validation and results

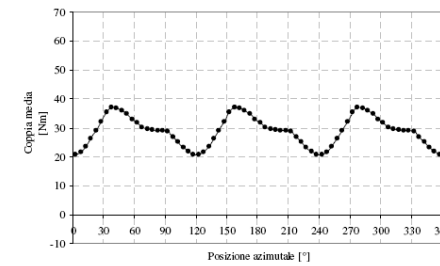
## Shaft torque and forces diagrams



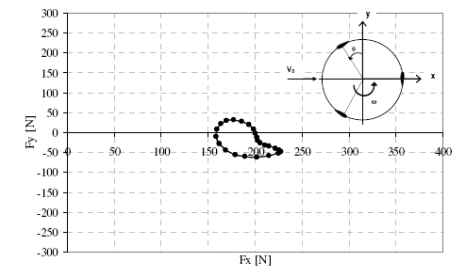
A1



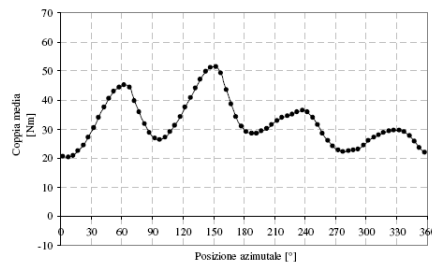
A2



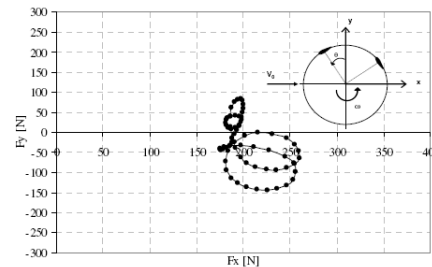
C1



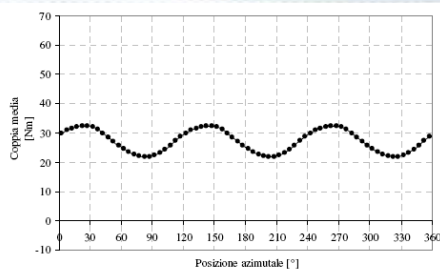
C2



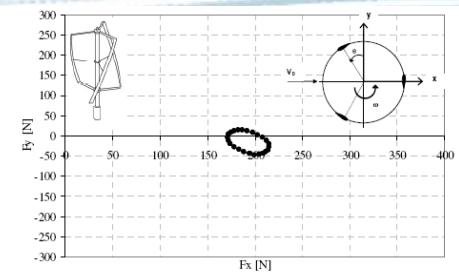
B1



B2



D1



D2

2-bladed presents the best power performance

3-bladed presents lower forces fluctuations

3-bladed Gorlov type presents the lowest fatigue loads (complex geometry)

2-bladed a 90° reduces the loads fluctuations but needs rotor balancing



# VAWT fluid dynamics

## Limitations of VAWT BEM codes

- The circular path is simplified in two actuator disks
- The momentum equilibrium is applied only in axial direction
- The axial expansion is generally neglected or not correctly/completely implemented
- The turbulent wake state correction is taken from HAWT corrections
- No (or weak) interaction between streamtubes
- Tip losses correction is of doubtful application for VAWT
- Complex geometry not resolvable from a fluid dynamic point of view
- Unsteady fluid dynamic effects are of difficult implementation



## Part II : VAWT analysis

### VAWT experimental analysis

VAWT experiments in controlled conditions

The Politecnico di Milano Large Wind Tunnel

High speed test section: 4x3.84m

Wind speed up to 55m/s

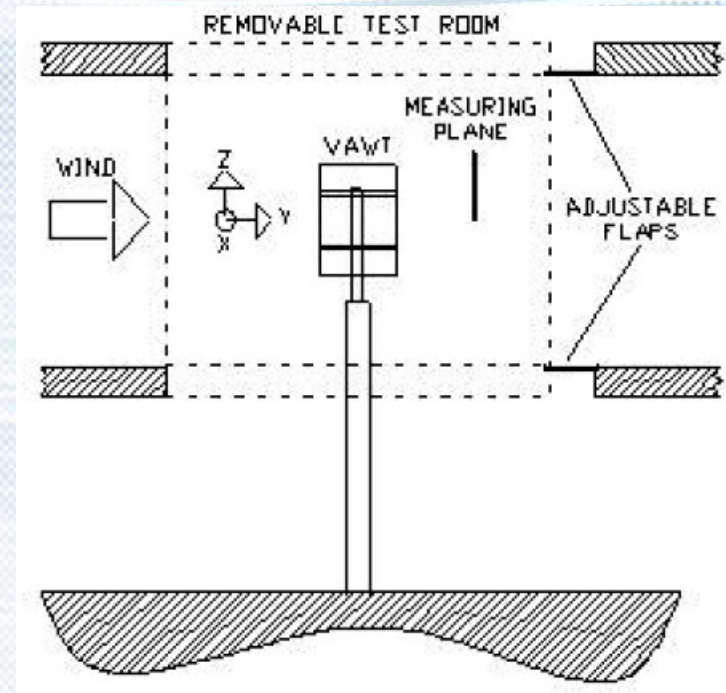
Possibility to work in open/close test section

2 different rotor prototypes designed by

Tozzi Nord Wind Turbines:

PDF1 – research purpose

PDF3 – commercial turbine





# The turbines layout and the instrumentations

## PDF1

3 Blades

H = 1.46m

D = 1.03m

NACA0021

Solidity 0.25

Rotor position

Torque

Support loads

## PDF3

3 Blades - Gorlov

H = 2.5m

D = 1.78m

P = 1.5kW

H(tower) = 3.5m

Rotor position

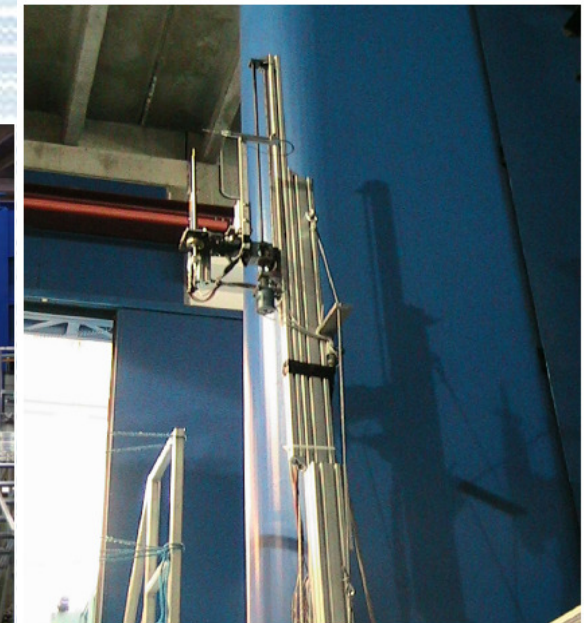
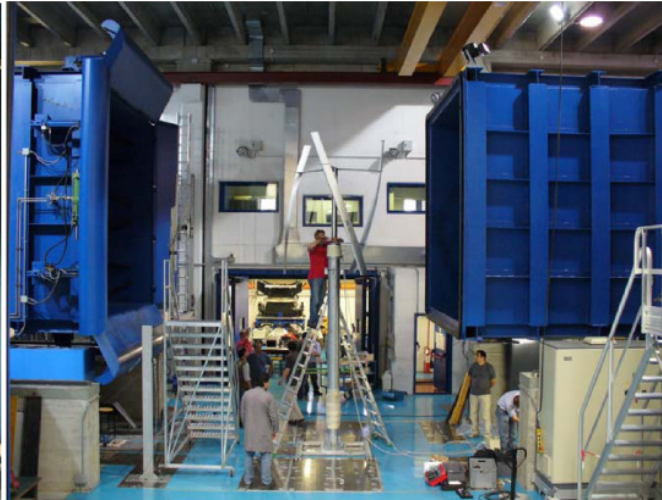
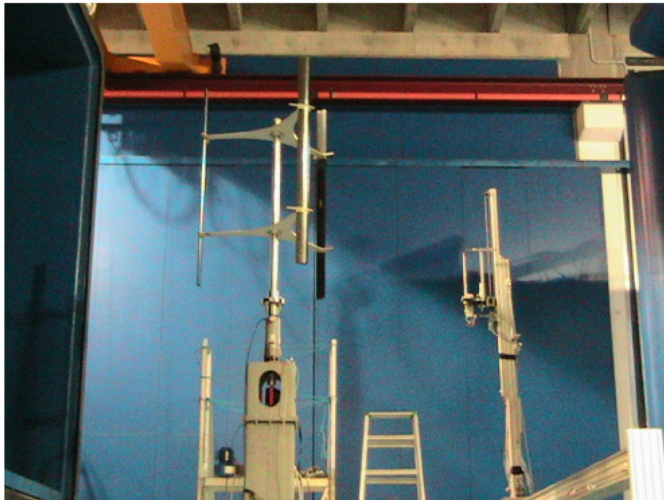
Torque (electric)

Support loads

## Aerodynamics

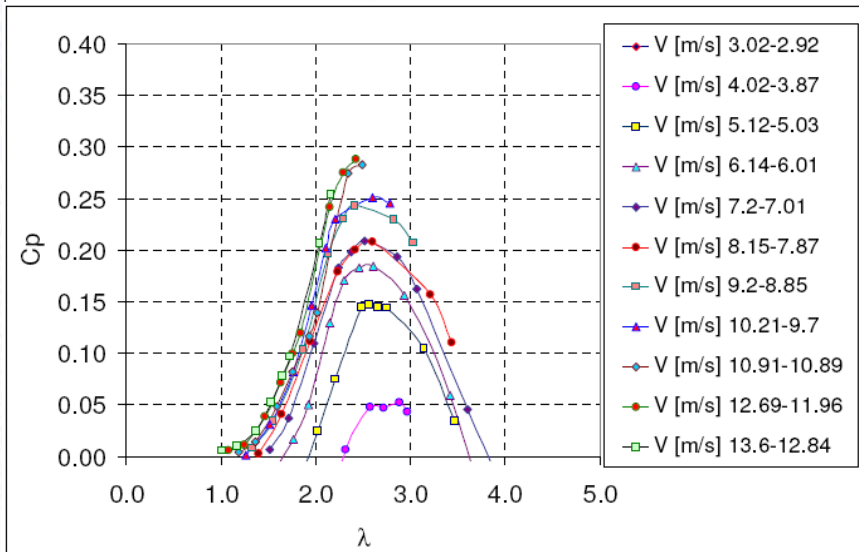
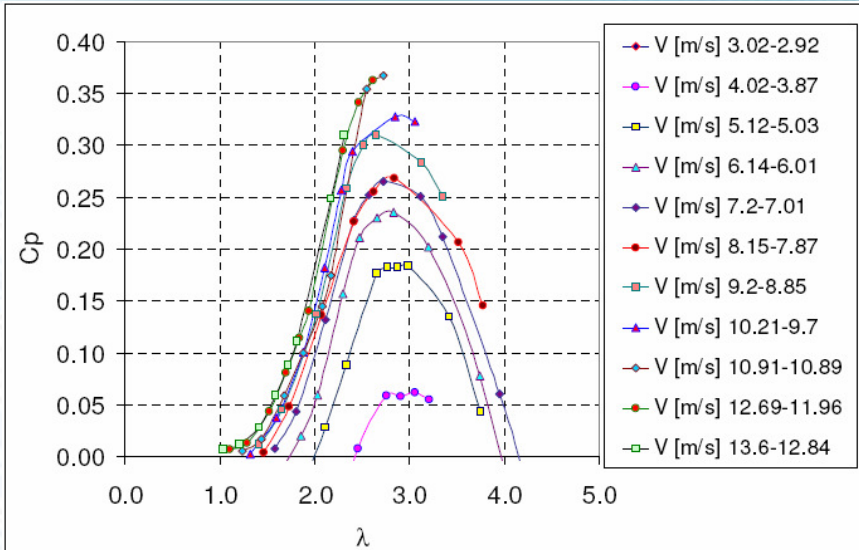
Directional pneumatic  
5 holes probe

Single sensor hot wire  
anemometer



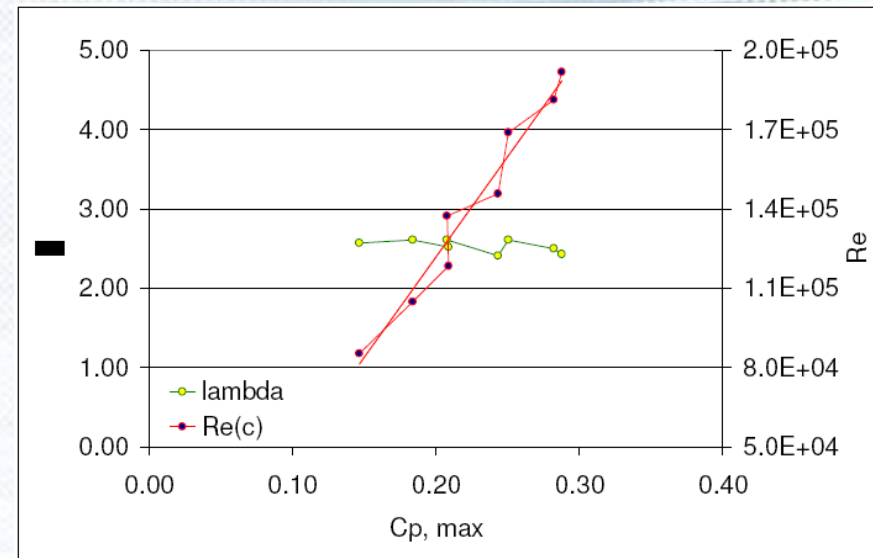


# VAWT experimental analysis PDF1 rotor - Performance



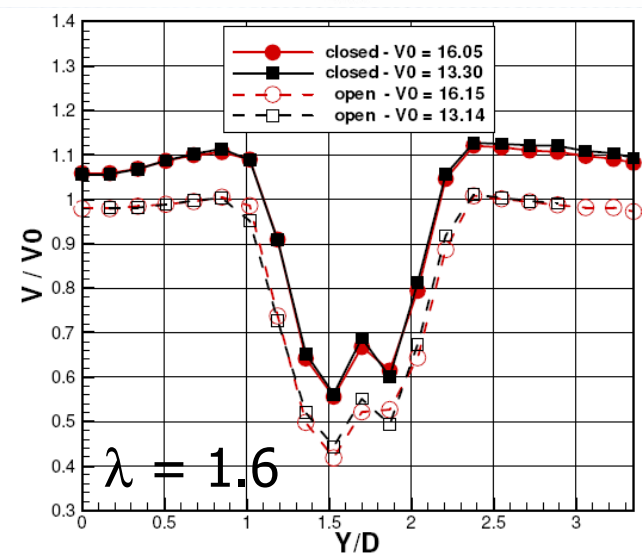
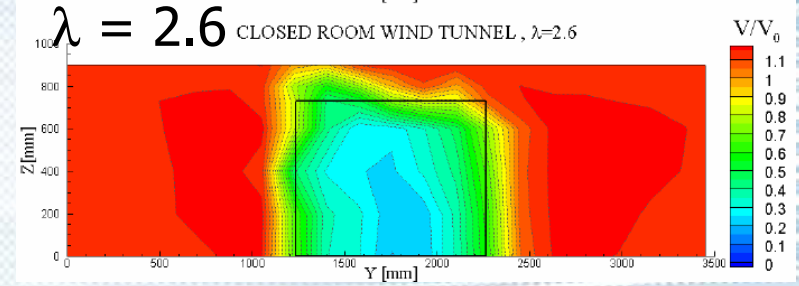
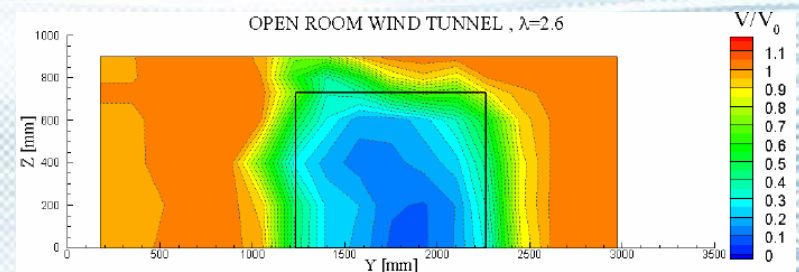
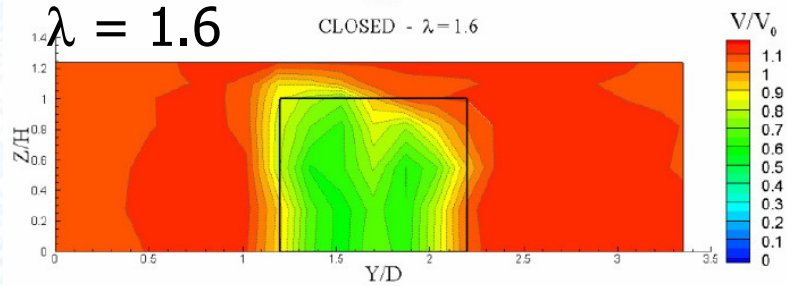
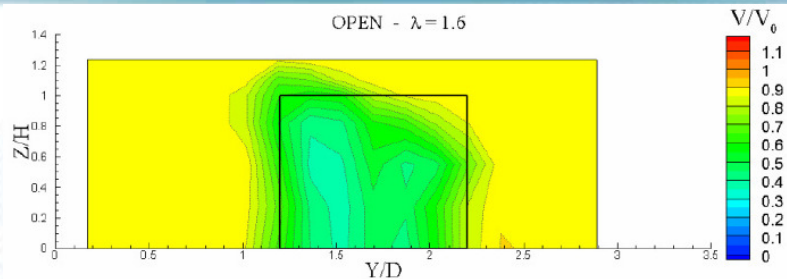
Blockage : 0.097 close test section  
Blockage effects up to 20-30% for  $C_p$  and 10-20% for  $C_T$

Reynolds numbers very important  
on power performance for  
 $Re < 200000$





# VAWT experimental analysis PDF1 rotor - Aerodynamics



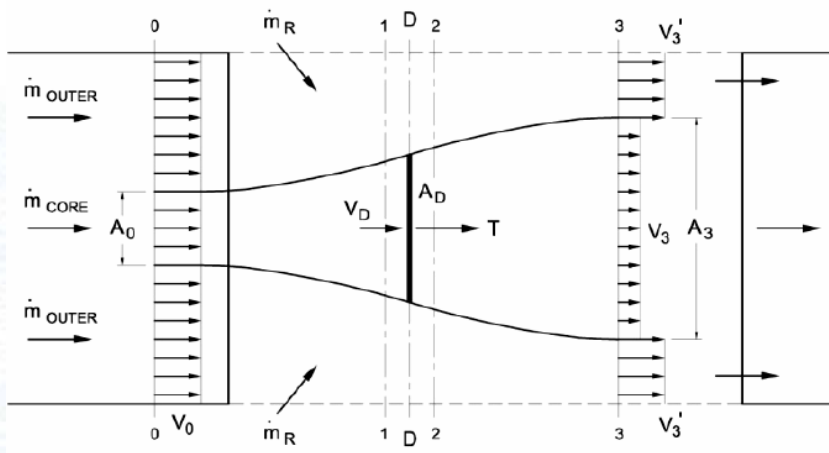
Wake non symmetric and deformed  
turnwise (in particular at low tip  
speed ratios)

In closed wind tunnel there is an  
higher velocity due to blockage  
effects





# VAWT experimental analysis PDF1 rotor - Aerodynamics

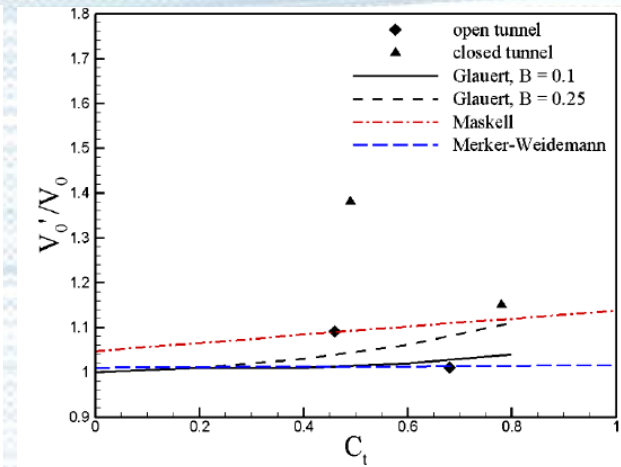
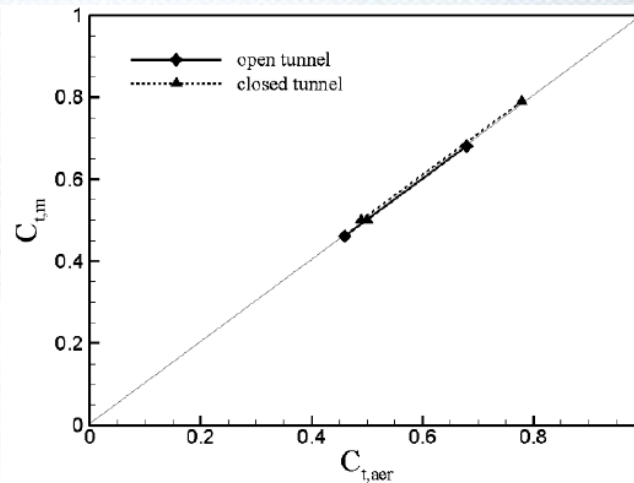
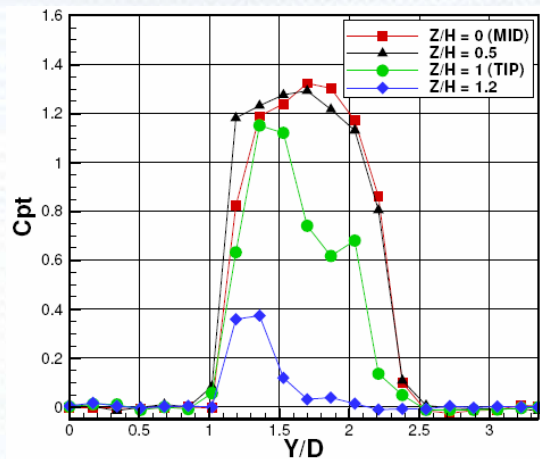


Wind tunnel blockage

$$T = A_D \left[ \left( p_0 + \frac{1}{2} \rho V_0^2 - \frac{1}{2} \rho V_D^2 \right) - \left( p_3 + \frac{1}{2} \rho V_3'^2 - \frac{1}{2} \rho V_D^2 \right) \right]$$

$$\frac{V_0'}{V_0} = \frac{V_D}{V_0} + \frac{C_T}{4} \frac{V_D}{V_0}$$

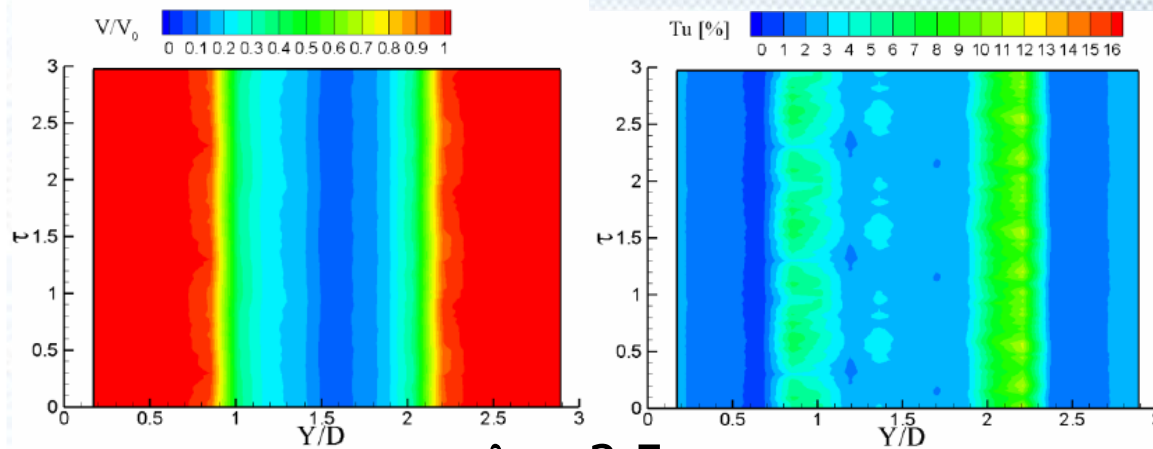
1D momentum theory doesn't seem  
the best model for blockage effects



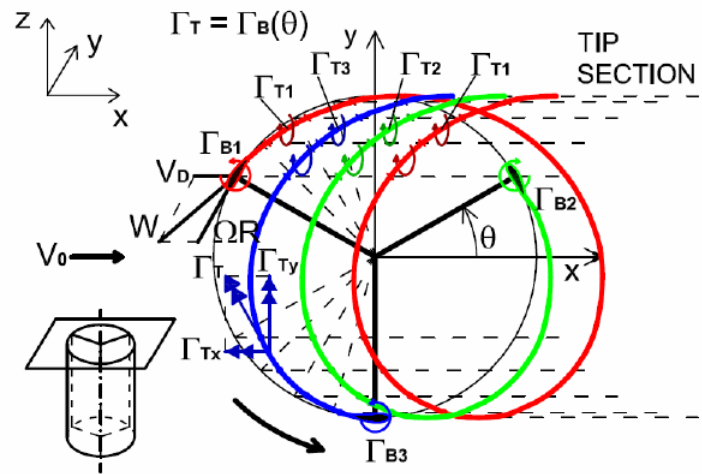
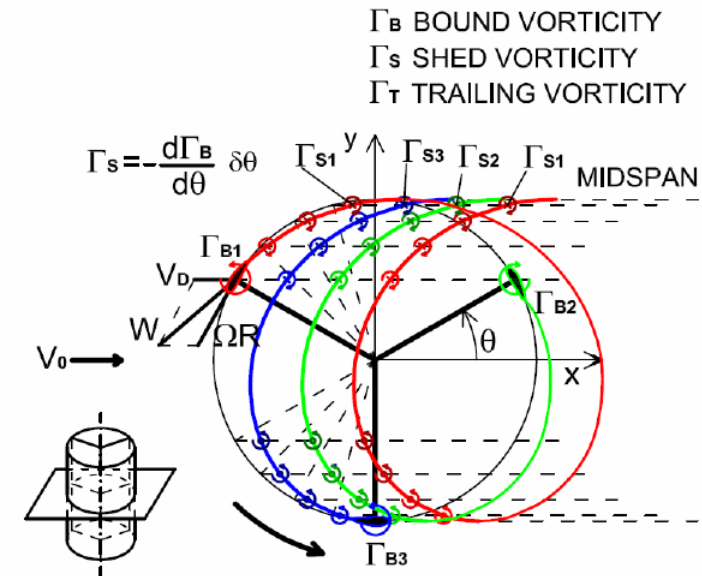
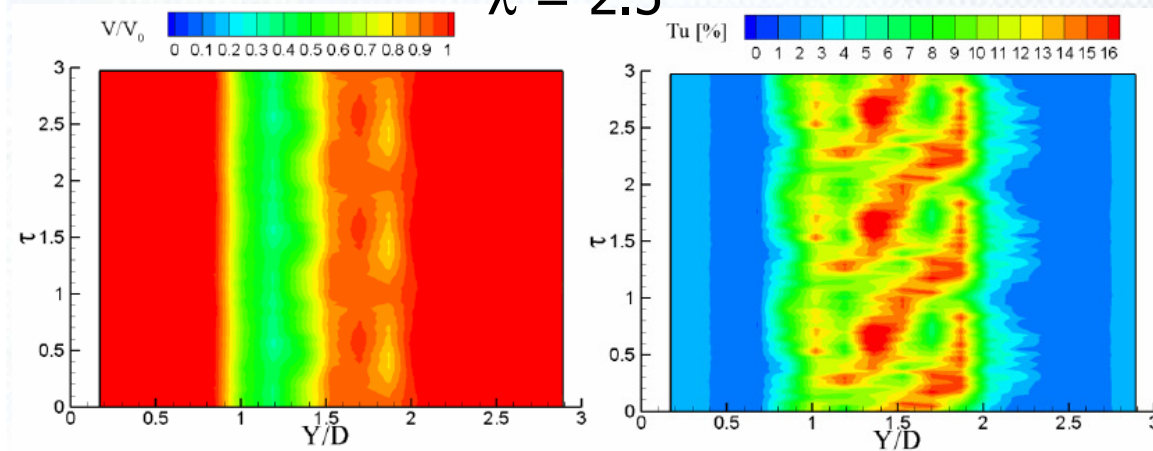


# VAWT experimental analysis PDF1 rotor - Aerodynamics

## Unsteady flow field



$\lambda = 2.5$

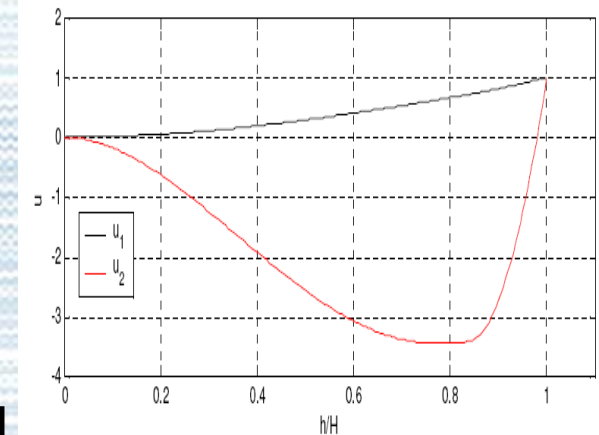
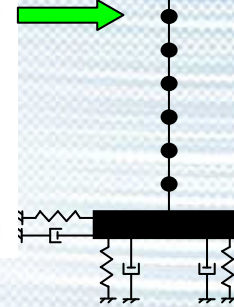
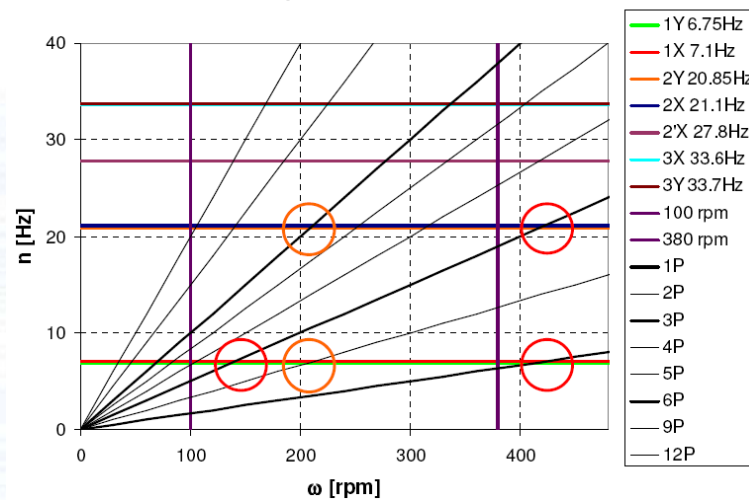




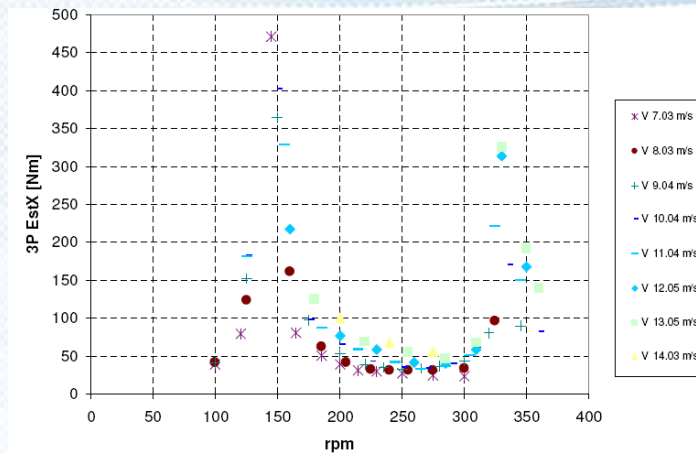
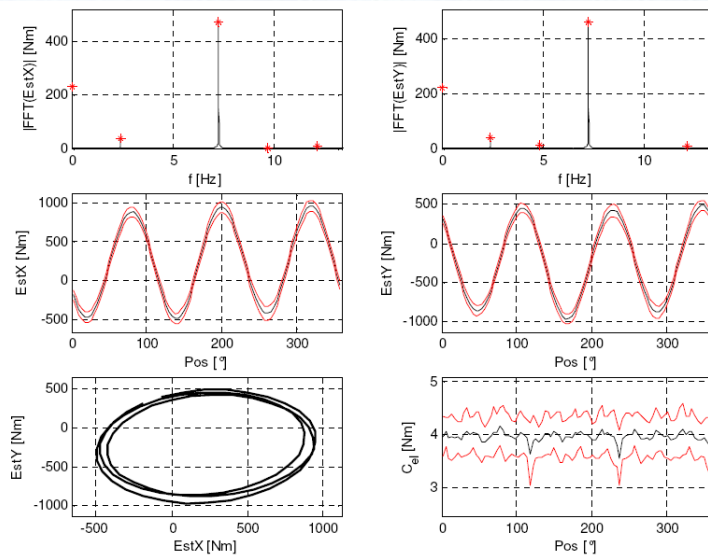
# VAWT experimental analysis

## PDF3 rotor - Dynamics

Diagramma di Campbell



## Dynamic analysis and modelling





# Part II : VAWT analysis

## 2D Free vortex wake

### Bound and shed vorticity

$$L = C_l \frac{1}{2} \rho W^2 c = \rho W \Gamma_B \quad \Gamma_B = \frac{1}{2} C_l W c \quad \delta \Gamma_S = -\frac{d\Gamma_B}{d\theta} \delta \theta$$

### Induced velocities (Biot-Savart)

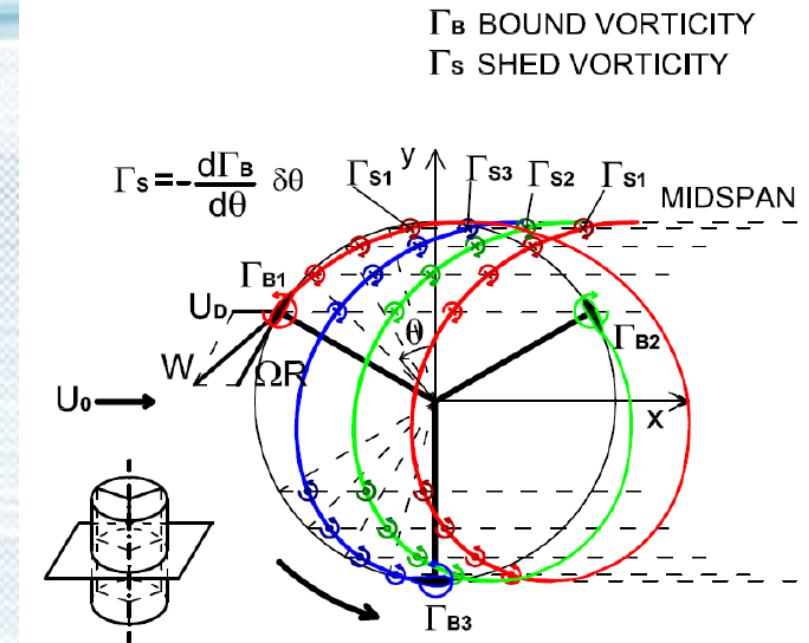
$$u = -\frac{\Gamma}{2\pi} \frac{(y - y_0)}{(x - x_0)^2 + (y - y_0)^2 + h^2} \quad v = \frac{\Gamma}{2\pi} \frac{(x - x_0)}{(x - x_0)^2 + (y - y_0)^2 + h^2}$$

### Flow characteristics

$$W^2 = [\Omega R + (U_0 + u_C) \cos(\theta) + v_C \sin(\theta)]^2 + [(U_0 + u_C) \sin(\theta) - v_C \cos(\theta)]^2$$

$$\phi = \tan^{-1} \frac{(U_0 + u_C) \sin(\theta) - v_C \cos(\theta)}{\Omega R + (U_0 + u_C) \cos(\theta) + v_C \sin(\theta)}$$

$$\alpha = \phi - \beta$$



### Shed vortex position

$$\tilde{x}_{S,i} = x_{S,i-1} + (U_0 + u_S(x_{S,i-1}, y_{S,i-1})) \cdot dt$$

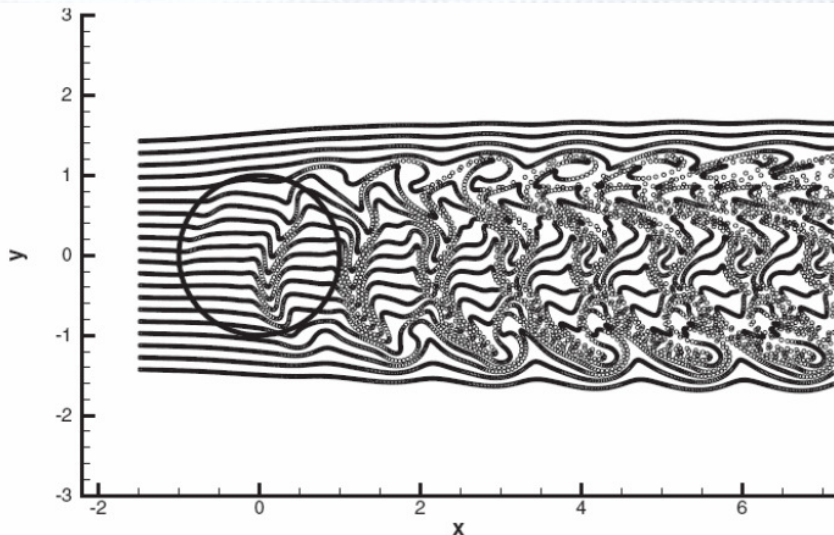
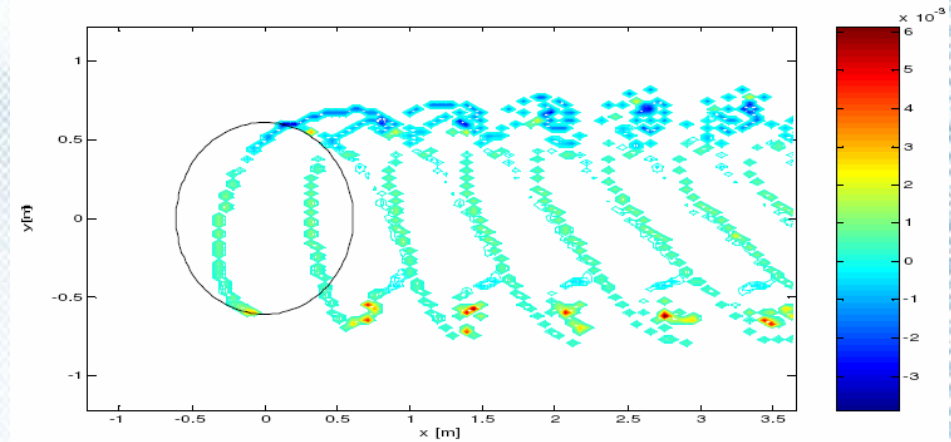
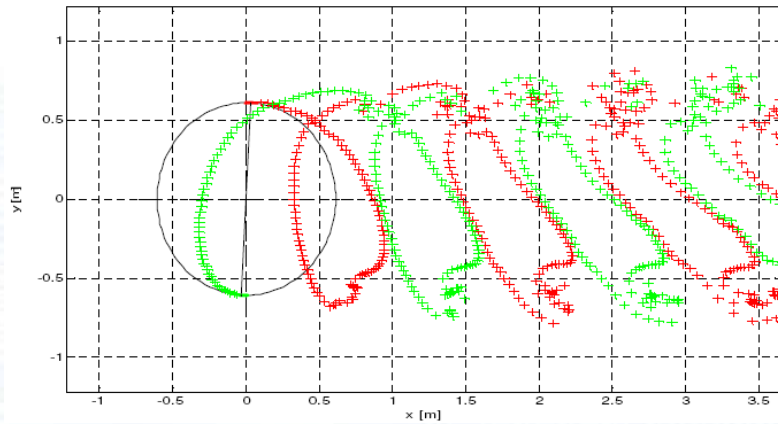
$$\tilde{y}_{S,i} = y_{S,i-1} + v_S(x_{S,i-1}, y_{S,i-1}) \cdot dt$$

$$x_{S,i} = x_{S,i-1} + \left[ U_0 + 0.5 \cdot (u_S(\tilde{x}_{S,i}, \tilde{y}_{S,i}) + u_S(x_{S,i-1}, y_{S,i-1})) \right] \cdot dt$$

$$y_{S,i} = y_{S,i-1} + 0.5 \cdot (v_S(\tilde{x}_{S,i}, \tilde{y}_{S,i}) + v_S(x_{S,i-1}, y_{S,i-1})) \cdot dt$$



# VAWT 2D Free vortex wake Validation and results

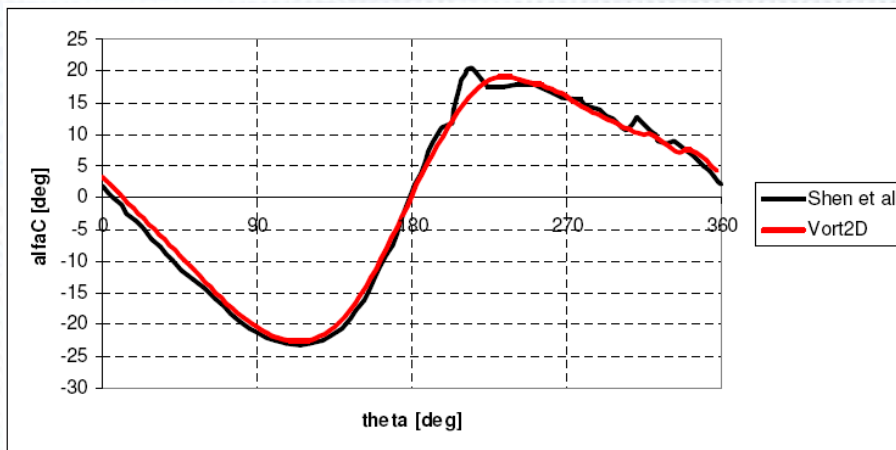
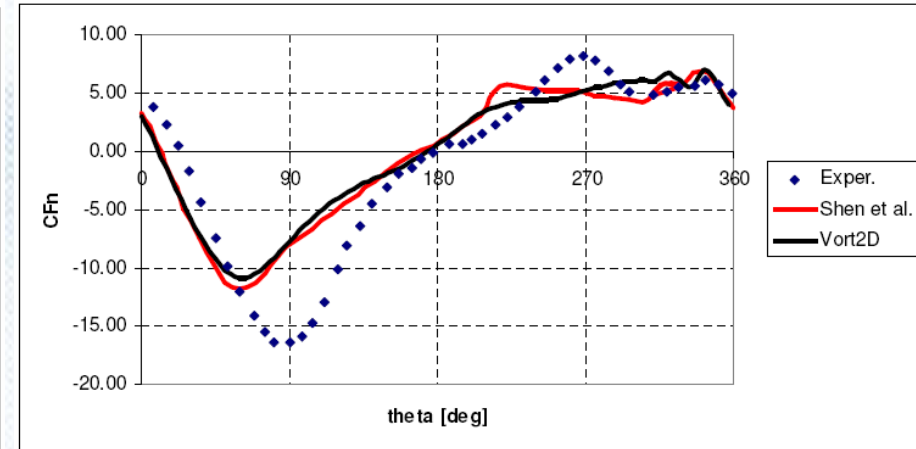
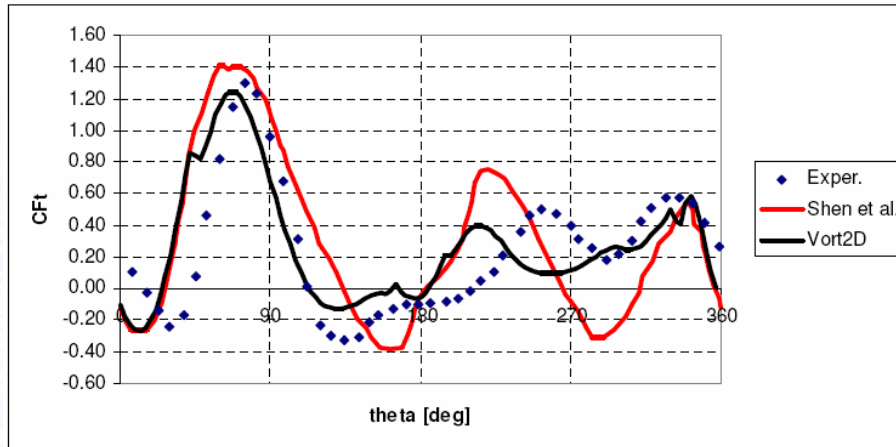


Comparison with Shen et al. actuator surface – CFD computations of a 2-bladed rotor

- Flow characteristics are qualitatively well assessed
- Viscosity is quite important



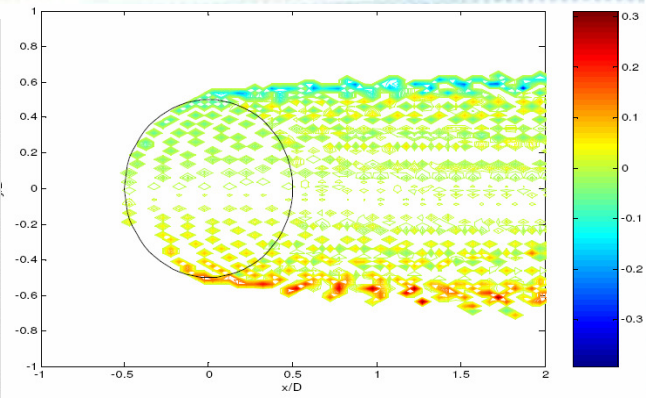
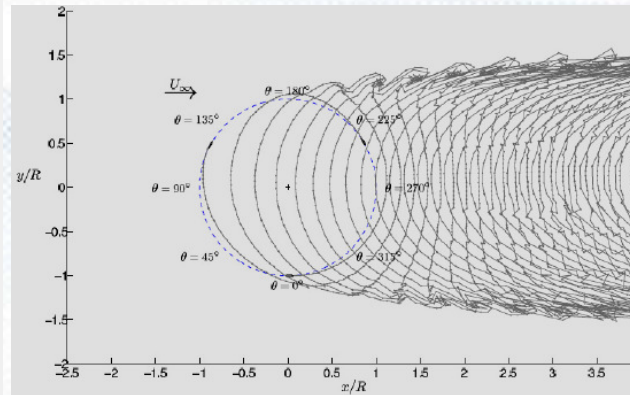
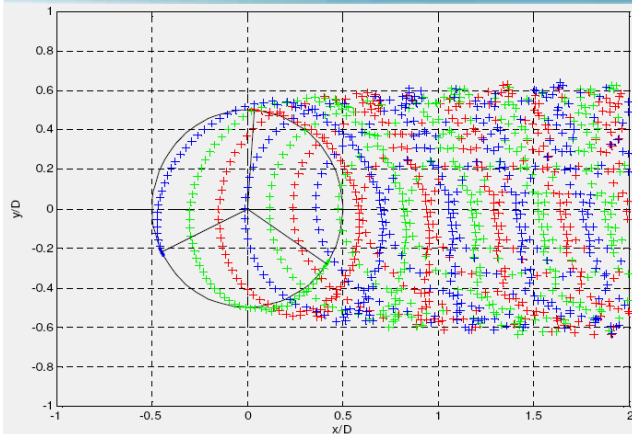
# VAWT 2D Free vortex wake Validation and results



- The angle of attack is well reproduced
- Airfoil database are very important
- Normal force coefficient peak not well reproduced: dynamic stall model to be improved



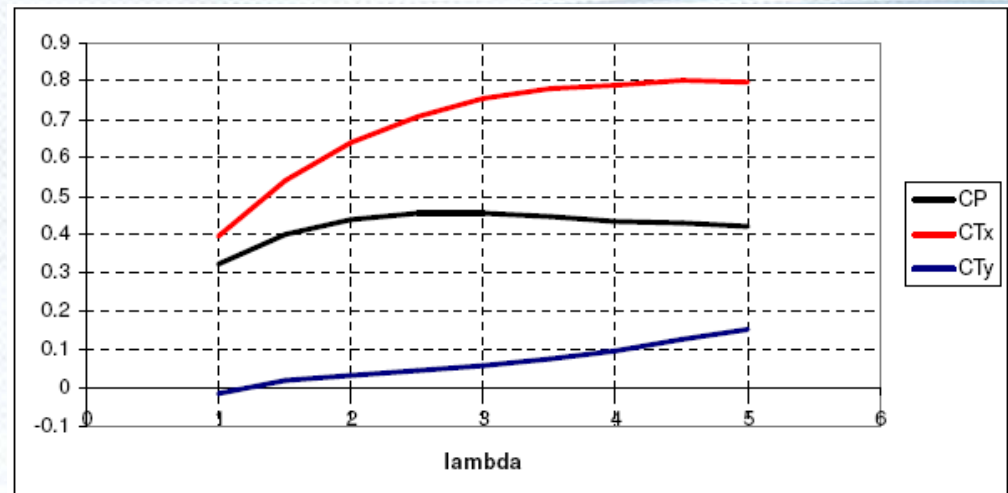
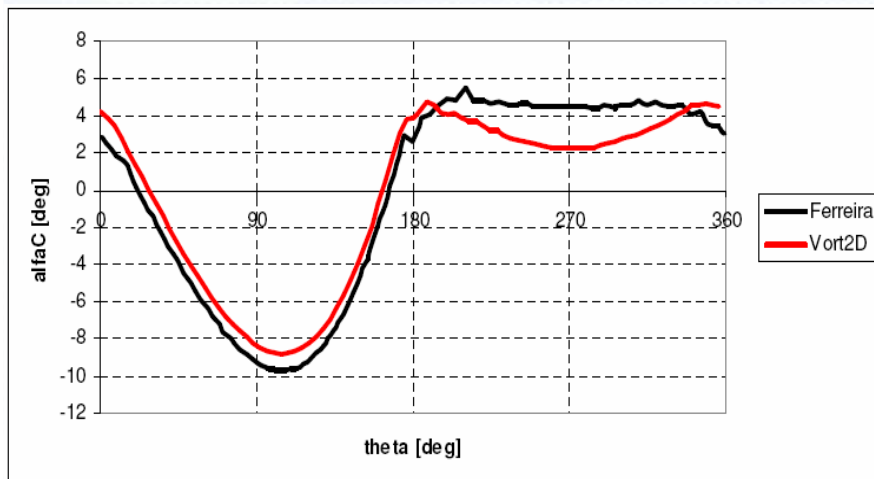
# Validation and results Ferreira panel model



The angle of attack is reproduced sufficiently well

The efficiency seems slightly lower than HAWT

Drag!





# Conclusions - HAWT

- HAWT analysis : actuator disk – momentum theory
- Shortcomings : swirl flow, wake expansion, tip effects
- General momentum theory can't overcome these issues
- Turbomachinery approach
- Radial equilibrium
- Radial equilibrium in meridional flow
- Turbomachinery approach + inverse design
- Innovative design should be found





# Conclusions - VAWT

- VAWT complex 3D geometry, working in his own wake
- VAWT analysis : double moultiple streamtubes – BEM model
- DMS-BEM limitations
- 2D free vortex wake
- Airfoil database + DS + tip correction
- Slightly lower efficiency
- Blockage effects and Reynolds numbers
- 1D momentum theory is not suited for VAWT - unsteady
- Structural dynamics : aeroelastic codes + free wake codes



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